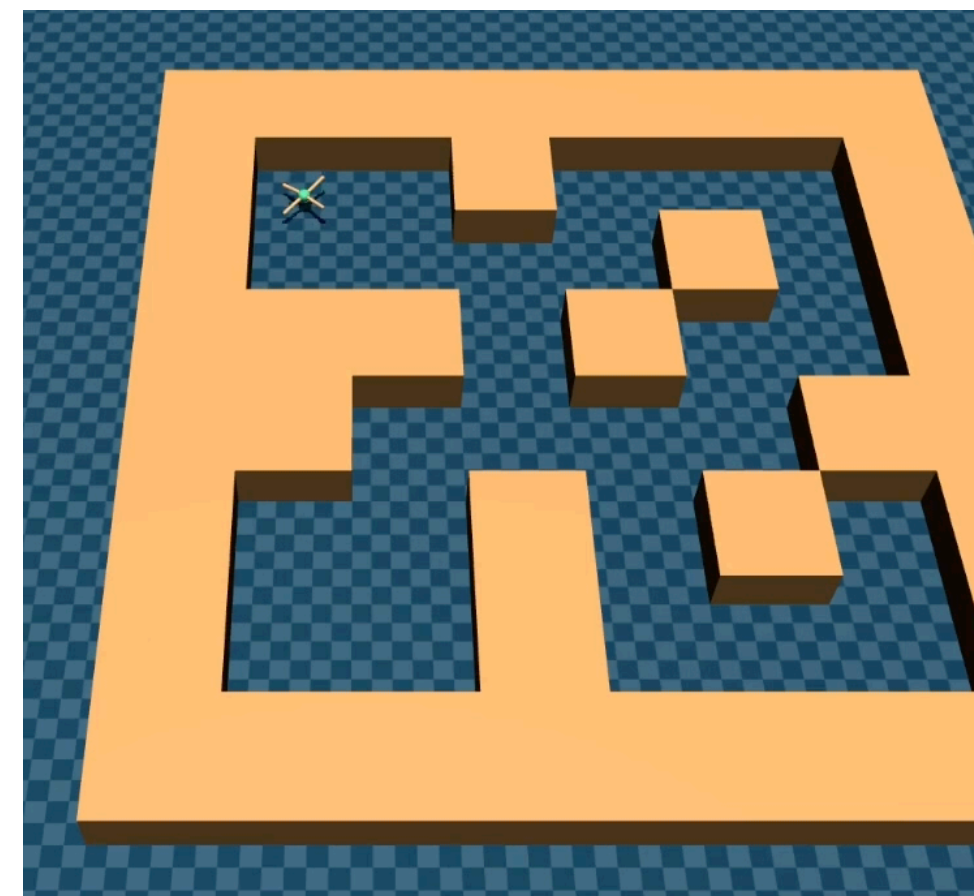


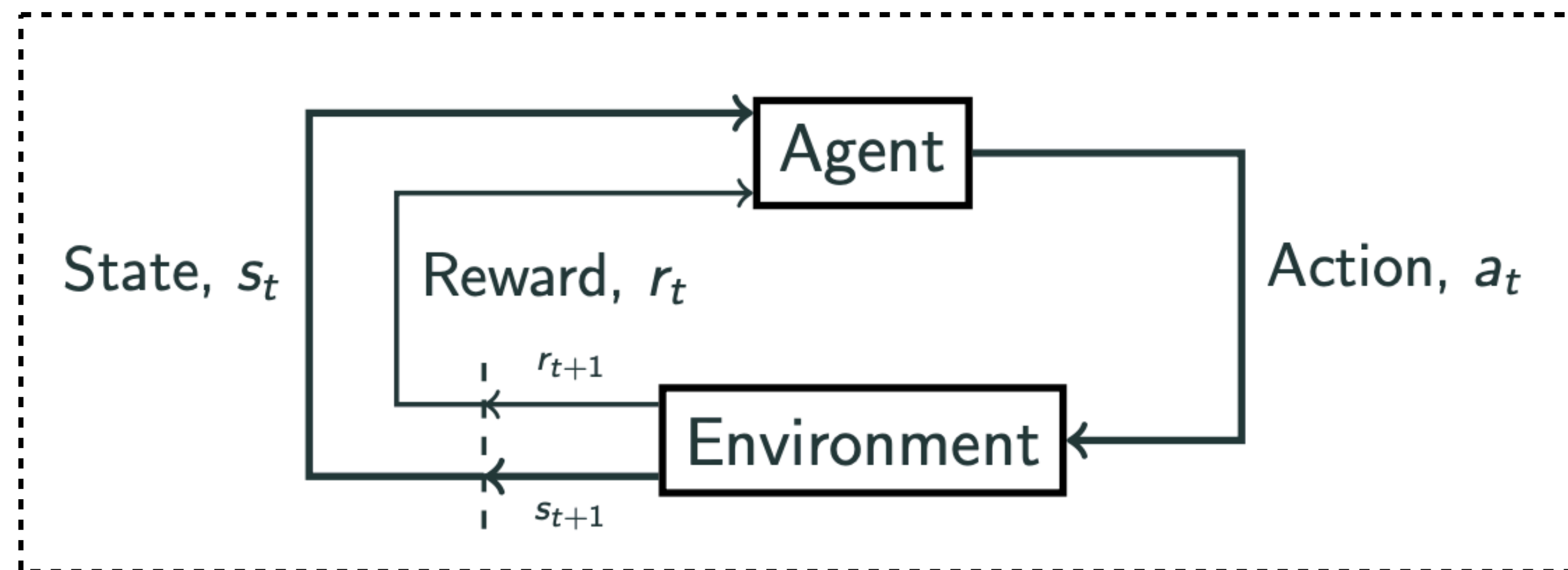
Entropy-regularized Diffusion Policy with Q-Ensembles for Offline RL

Ruoqi Zhang, Ziwei Luo, Jens Sjölund, Thomas Schön, Per Mattsson



Offline Reinforcement Learning

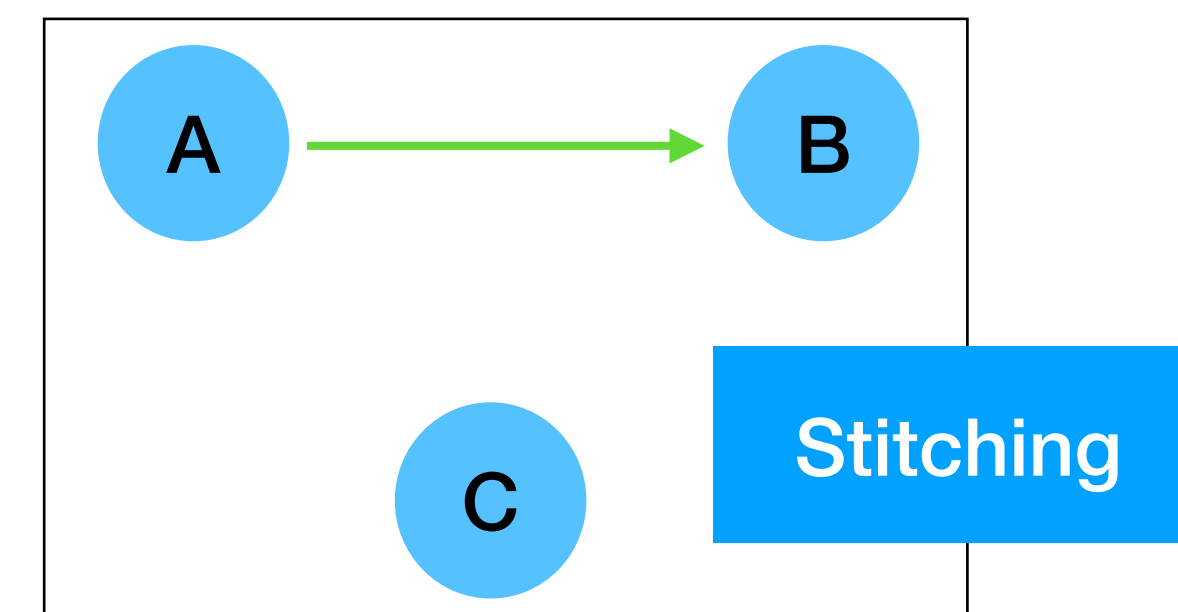
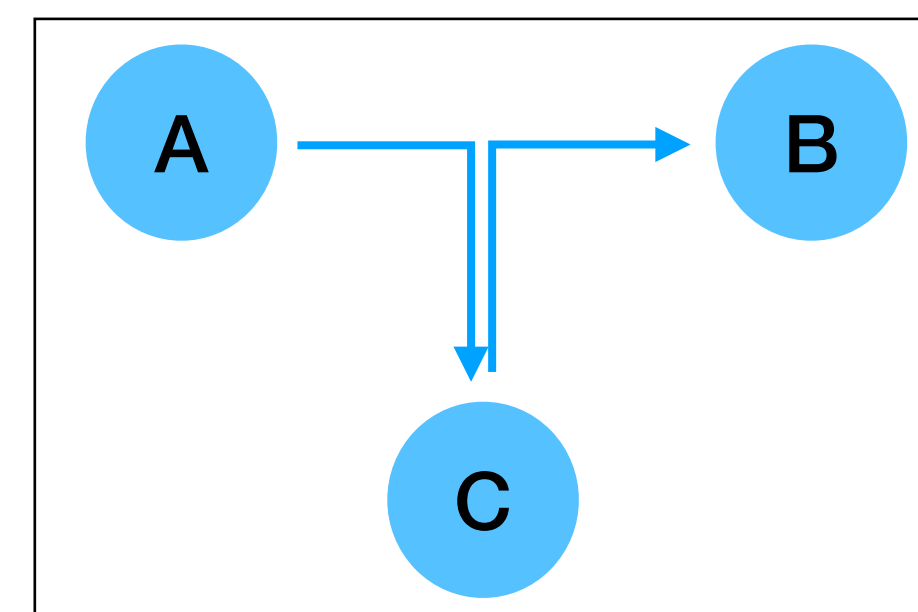
Learning from the dataset only



Dataset \mathcal{D}

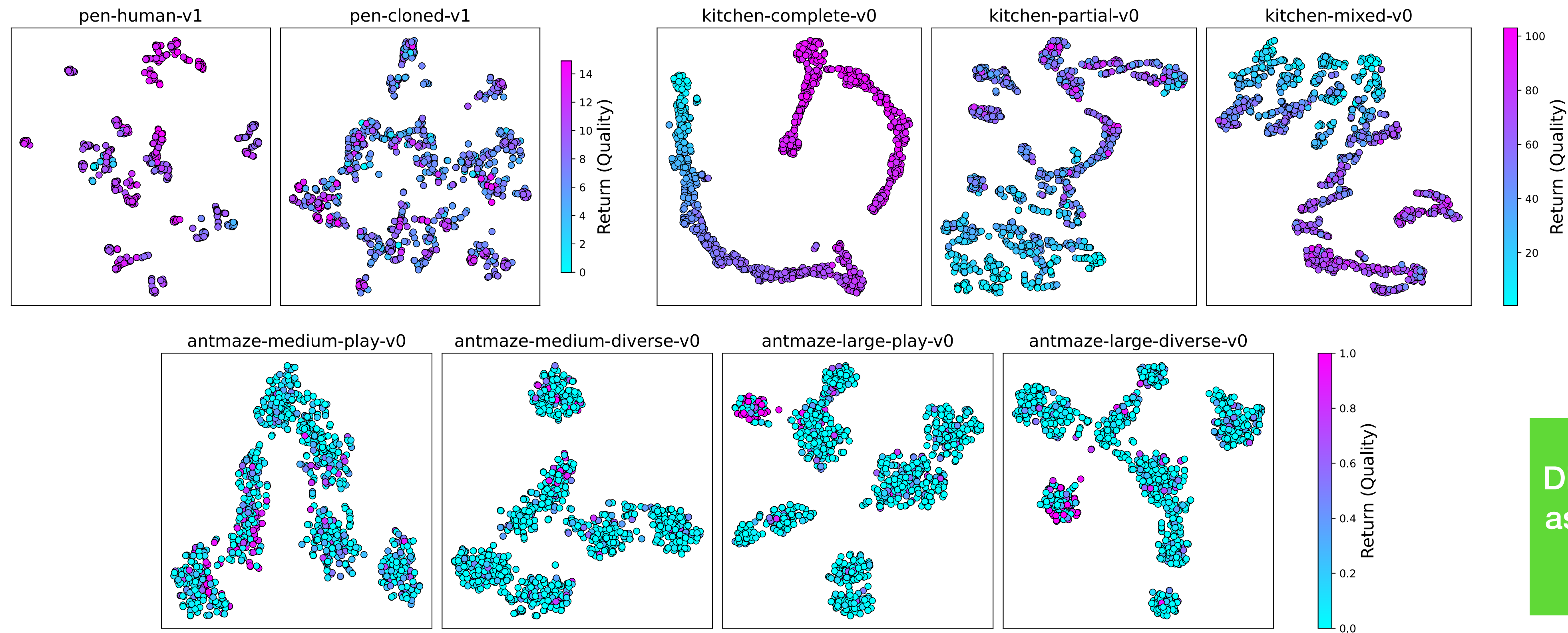
Do better than the dataset!

Policy: $a_t = \pi_{\theta}(s_t) = \arg \max_a \mathbb{E} \left[\sum_{k=0}^{\infty} \gamma^k r_{t+k+1} \right]$



Offline Reinforcement Learning

Multi-modality of the Dataset: t-SNE visualization



Diffusion model
as the behavior
policy

Figure 1. A t-SNE visualization of randomly selected 1000 states from Antmaze, Adroit and Kitchen domain. The color coding represents the return of the trajectory associated with each state.



- **Diffusion-QL [1]:** Diffusion Model as the behaviour policy

$$\pi = \arg \min_{\pi_\phi} L(\phi) = \mathcal{L}_d(\phi) + \mathcal{L}_q(\phi) = \mathcal{L}_d(\phi) - \lambda \cdot \mathbb{E}_{s \sim \mathcal{D}, a^0 \sim \pi_\phi} [Q_\psi(s, a^0)]$$

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Out-of-distribution state & actions?

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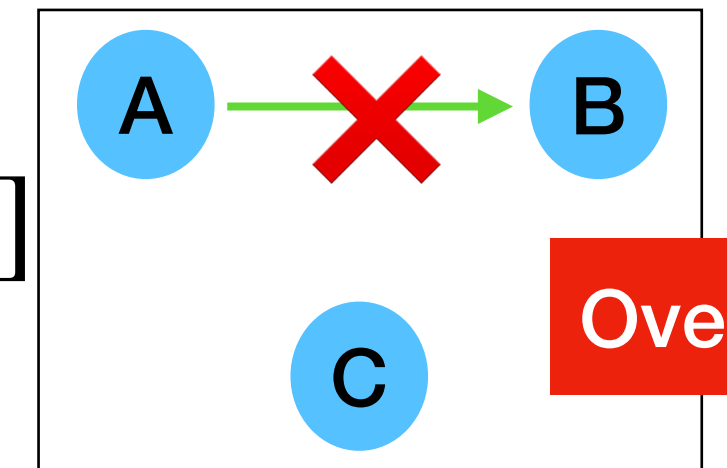
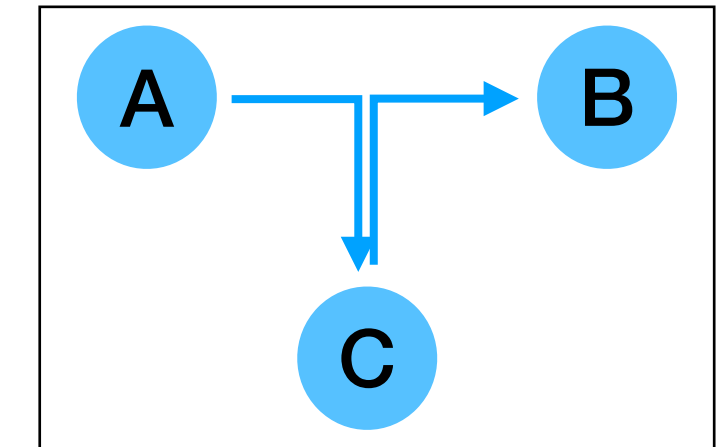
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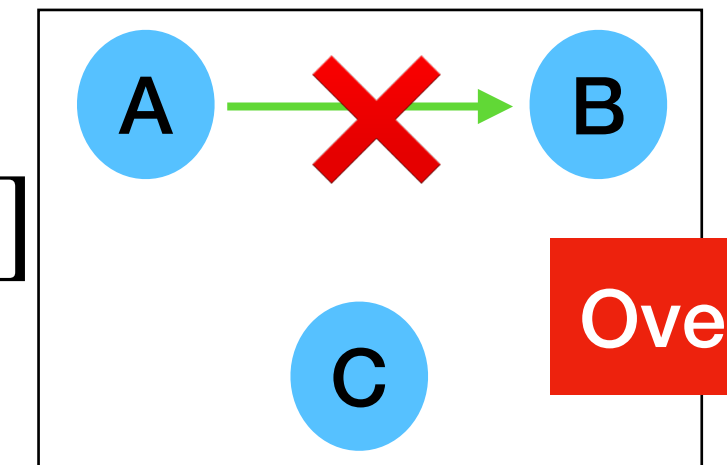
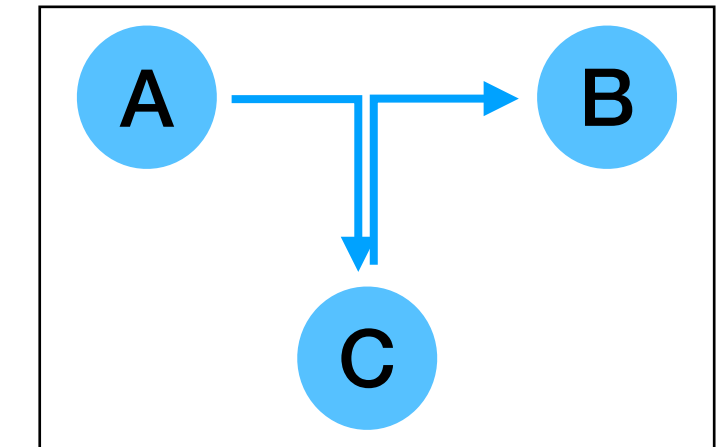


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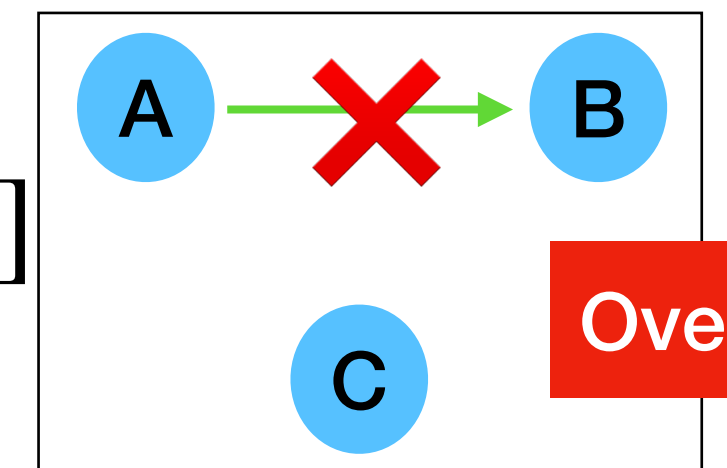
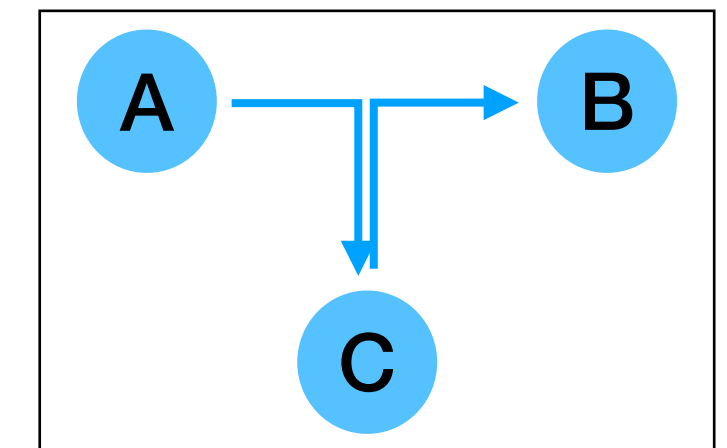
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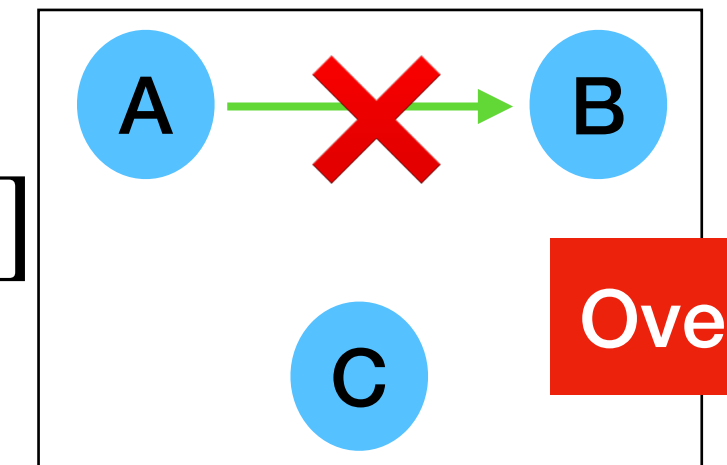
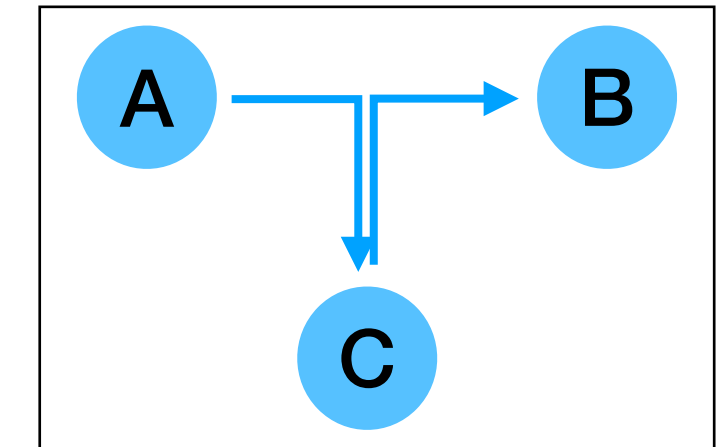
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$$\begin{aligned} \text{SAC[2]: } \pi^* &= \arg \max_{\pi} \sum_t \mathbb{E}_{(s_t, \mathbf{a}_t) \sim \rho_\pi} \left[r(s_t, \mathbf{a}_t) + \alpha \mathcal{H}(\pi(\cdot | s_t)) \right] \\ &= \arg \min J_\pi(\phi) = \mathbb{E}_{s_t \sim \mathcal{D}} \left[\mathbb{E}_{\mathbf{a}_t \sim \pi_\phi} \left[\alpha \log(\pi_\phi(\mathbf{a}_t | s_t)) - Q_\psi(s_t, \mathbf{a}_t) \right] \right] \end{aligned}$$

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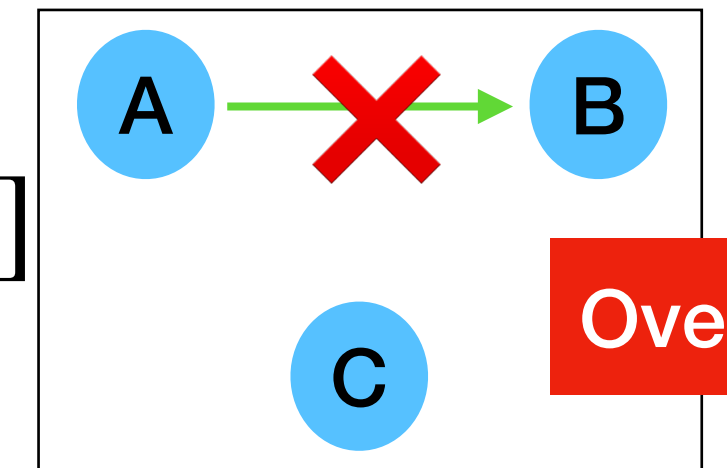
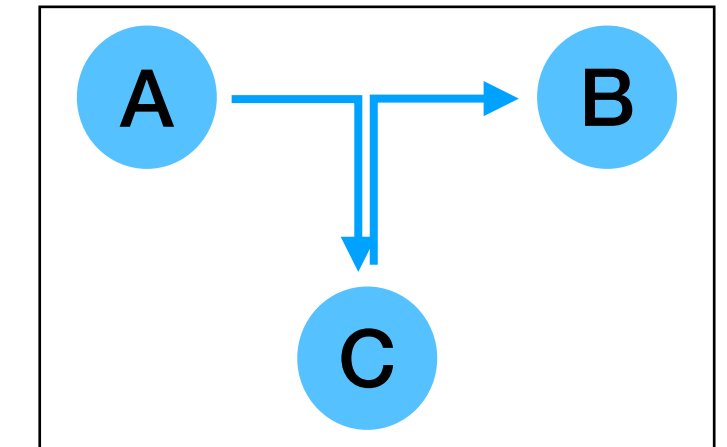
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Overfitting!

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LCB of Q-
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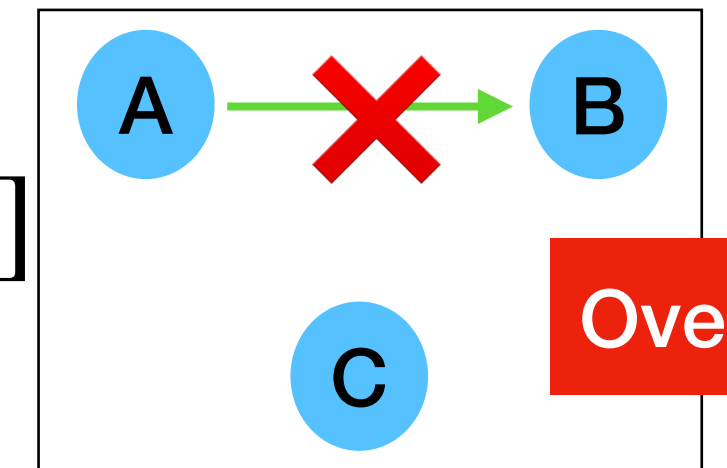
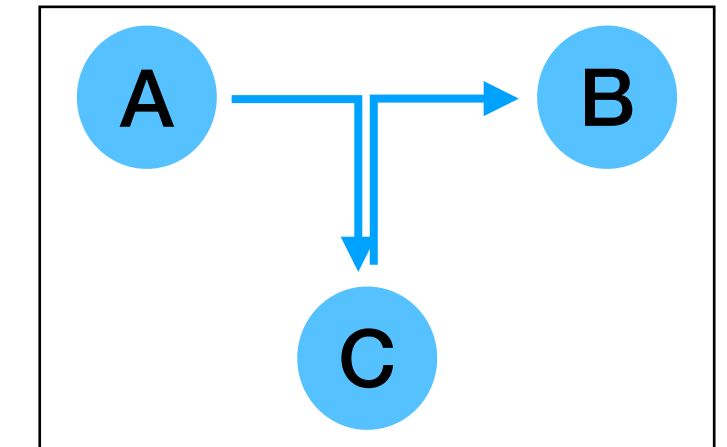
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$$Q_{\psi}^{\text{LCB}} = \mathbb{E}_{\text{ens}} [Q_{\psi^m}(s, a)] - \beta \left[\sqrt{\mathbb{V}_{\text{ens}}[Q_{\psi^m}(s, a)]} \right]$$



Overfitting!

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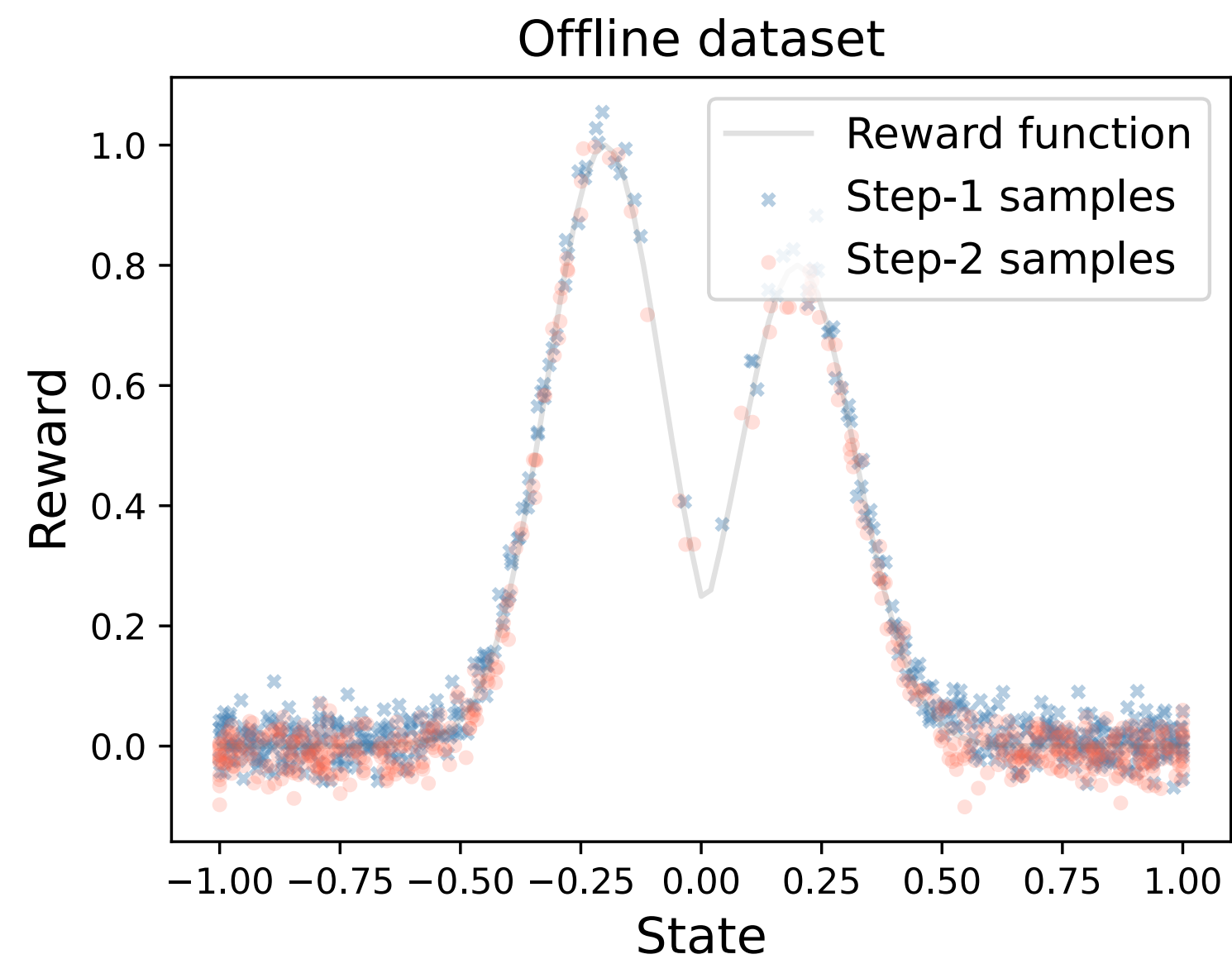
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Diffusion Policy

Task: Starting from 0, take two steps to seek a state with the highest reward.



(a)



Diffusion Policy

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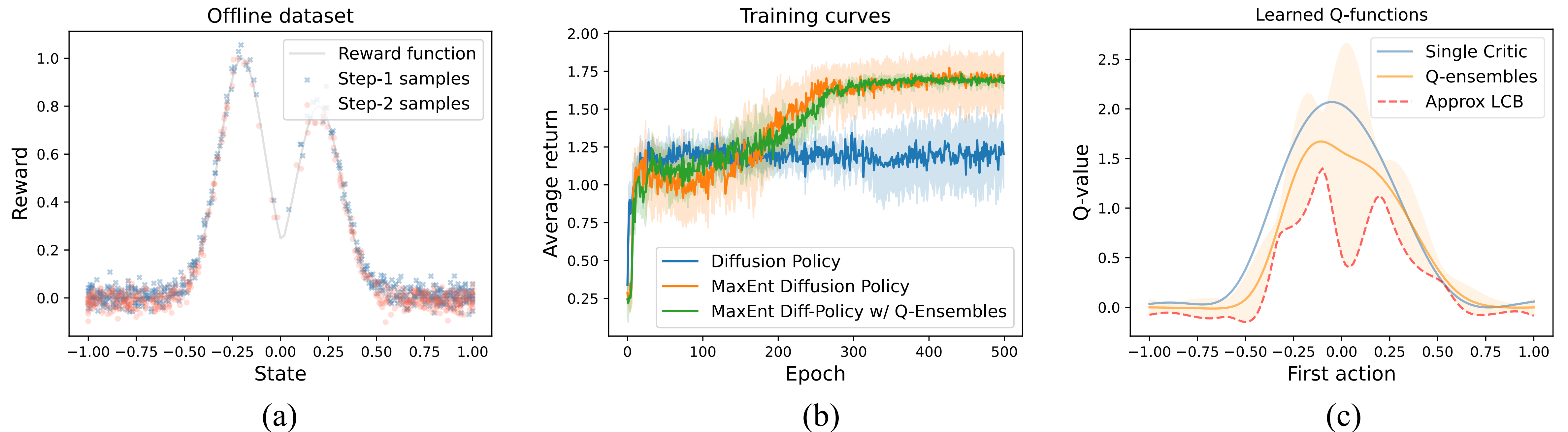
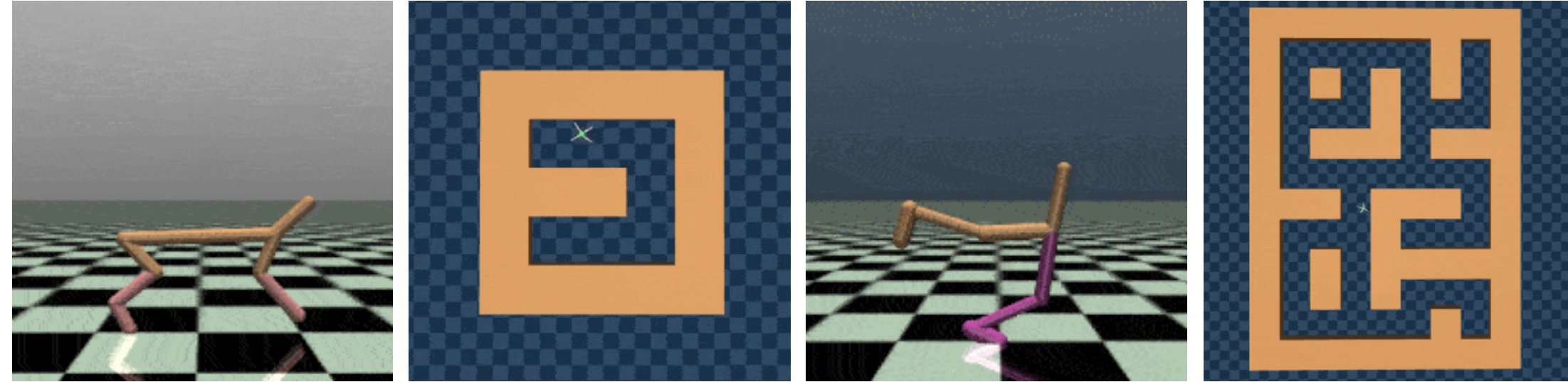


Figure 3. Left: Reward function and training samples **Center:** Training progress comparison **Right:** Learned Q-values curve in state 0 **Take-away:** Only combined entropy+diffusion+ensembles learn a better policy and accurate Q-values. [2]

Experiments: D4RL

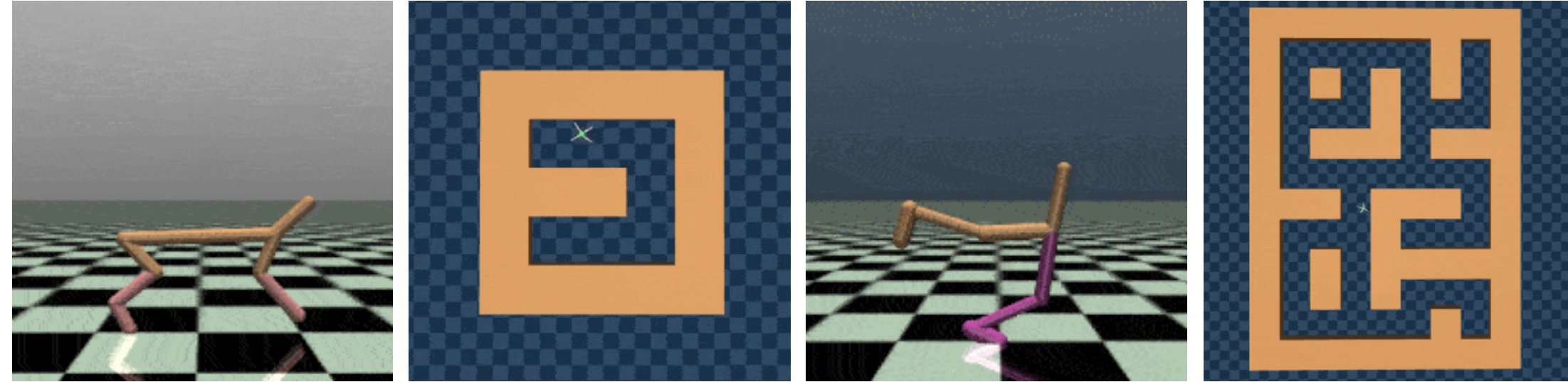


GYM TASKS	BC	DT	CQL	IQL	IDQL-A	IQL+EDP	DIFF-QL	OURS
HALFCHEETAH-MEDIUM-V2	42.6	42.6	44.0	47.4	51.0	48.1	51.1	54.9
HOPPER-MEDIUM-V2	52.9	67.6	58.5	66.3	65.4	63.1	90.5	94.2
WALKER2D-MEDIUM-V2	75.3	74.0	72.5	78.3	82.5	85.4	87.0	92.5
HALFCHEETAH-MEDIUM-REPLAY-V2	36.6	36.6	45.5	44.2	45.9	43.8	47.8	57.0
HOPPER-MEDIUM-REPLAY-V2	18.1	82.7	95.0	94.7	92.1	99.1	101.3	102.7
WALKER2D-MEDIUM-REPLAY-V2	26.0	66.6	77.2	73.9	85.1	84.0	95.5	94.20
HALFCHEETAH-MEDIUM-EXPERT-V2	55.2	86.8	91.6	86.7	95.9	86.7	96.8	90.32
HOPPER-MEDIUM-EXPERT-V2	52.5	107.6	105.4	91.5	108.6	99.6	111.1	111.9
WALKER2D-MEDIUM-EXPERT-V2	107.5	108.1	108.8	109.6	112.7	109.0	110.1	111.2
AVERAGE	51.9	74.7	77.6	77.0	82.1	79.9	88.0	89.9

ANTMAZE TASKS	BC	DT	CQL	IQL	MSG	IDQL-A	IQL+EDP	DIFF-QL	OURS
ANTMAZE-UMAZE-V0	54.6	59.2	74	87.5	97.8	94.0	87.5	93.4	100
ANTMAZE-UMAZE-DIVERSE-V0	45.6	53.0	84.0	62.2	81.8	80.2	62.2	66.2	79.8
ANTMAZE-MEDIUM-PLAY-V0	0.0	0.0	61.2	71.2	89.6	84.5	71.2	76.6	91.4
ANTMAZE-MEDIUM-DIVERSE-V0	0.0	0.0	53.7	70.0	88.6	84.8	70.0	78.6	91.6
ANTMAZE-LARGE-PLAY-V0	0.0	0.0	15.8	39.6	72.6	63.5	39.6	46.4	81.2
ANTMAZE-LARGE-DIVERSE-V0	0.0	0.0	14.9	47.5	71.4	67.9	47.6	56.6	76.4
AVERAGE	16.7	18.7	50.6	63.0	83.6	79.1	63.0	69.6	86.7



Experiments: D4RL

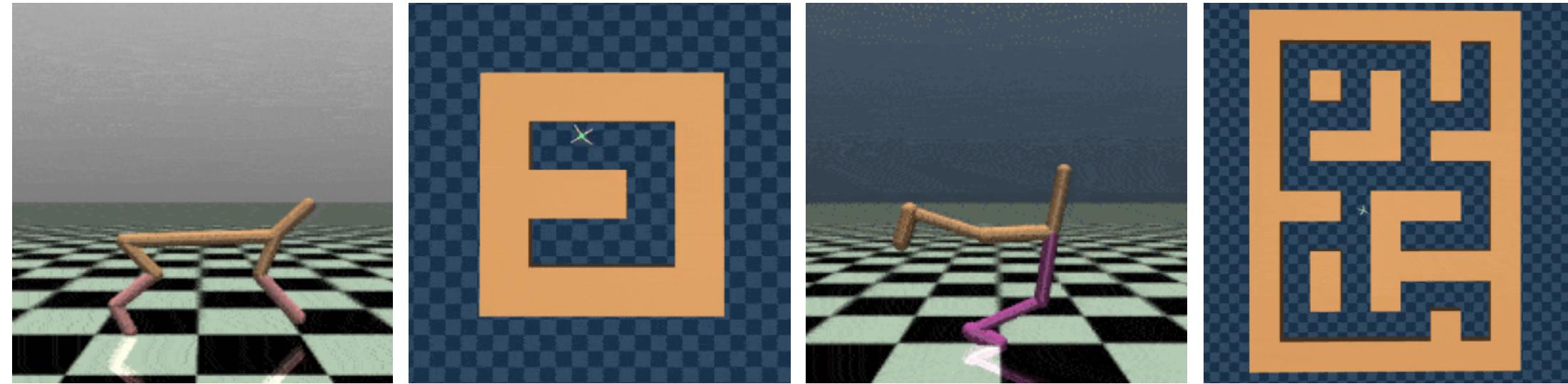


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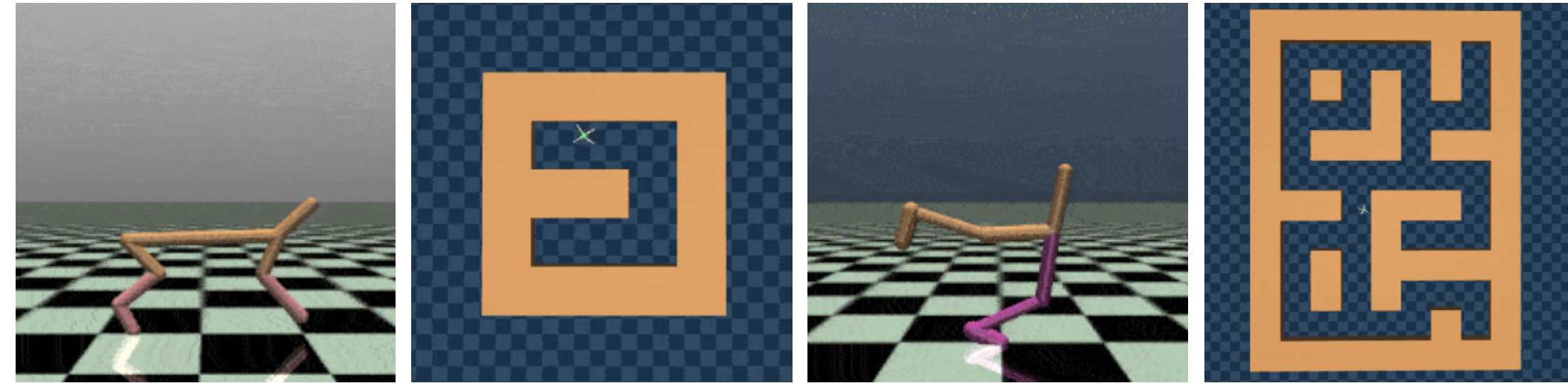
Experiments: D4RL



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ANTMAZE-UMAZE-V0	54.6	59.2	74	87.5	97.8	94.0	87.5	93.4	100		
ANTMAZE-UMAZE-DIVERSE-V0	45.6	53.0	84.0	62.2	81.8	80.2	62.2	66.2	79.8		
ANTMAZE-MEDIUM-PLAY-V0	0.0	0.0	61.2	71.2	89.6	84.5	71.2	76.6	91.4		
ANTMAZE-MEDIUM-DIVERSE-V0	0.0	0.0	53.7	70.0	88.6	84.8	70.0	78.6	91.6		
ANTMAZE-LARGE-PLAY-V0	0.0	0.0	15.8	39.6	72.6	63.5	39.6	46.4	81.2		
ANTMAZE-LARGE-DIVERSE-V0	0.0	0.0	14.9	47.5	71.4	67.9	47.6	56.6	76.4		
AVERAGE	16.7	18.7	50.6	63.0	83.6	79.1	63.0	69.6	86.7		

↑24%

