

Clustering with Non-adaptive Subset Queries

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Clustering via Crowdsourcing

Clustering: group data based on similarity

- Fundamental task in data science with many instantiations

Clustering via crowdsourcing:

- Can we offload the work of computing a clustering by asking simple questions to external individuals?
- **Same-cluster queries:** Are these two points of the same type?



Are these animals in the same genus?



Yes!

Clustering via Crowdsourcing

Clustering: group data based on similarity

- Fundamental task in data science with many instantiations

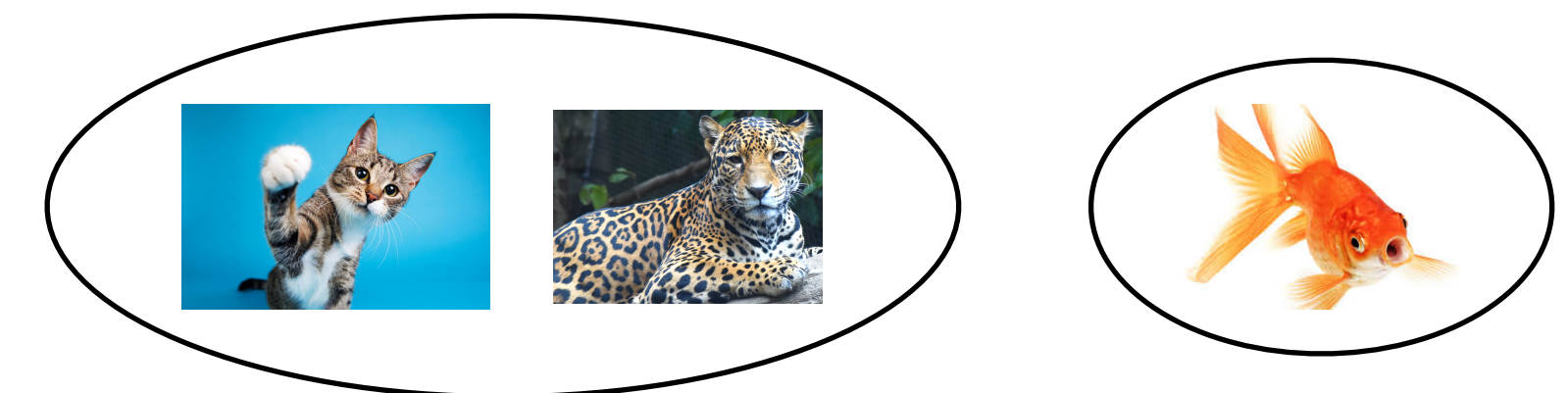
Clustering via crowdsourcing:

- Can we offload the work of computing a clustering by asking simple questions to external individuals?
- **Same-cluster queries:** Are these two points of the same type?

Wish list: (1) few queries, (2) queries specified in few rounds

- Spongebob & Squidward might be slow
⇒ Want to parallelize queries
- **Ideally:** non-adaptive (queries specified in one round)

Query profile



Learned clustering

Clustering via Same-Cluster Queries

Mazumdar-Saha [Neurips 17], Mazumdar-Saha [AAAI 17], Mazumdar-Pal [Neurips 17], Mitzenmacher-Tsouraskis [16], Saha-Subramanian [ESA 19], Pia-Ma-Tzamos [COLT 22], Bressan-Cesa-Bianchi-Lattanzi-Paudice [Neurips 20], Huleihal-Mazumdar-Médard-Pal [Neurips 19]

- Set U of n points with hidden partition $C_1 \sqcup \dots \sqcup C_k = U$
- Can **query** any $\{x, y\} \subset U$
 - Oracle says **YES** if x, y in same cluster and **NO** otherwise

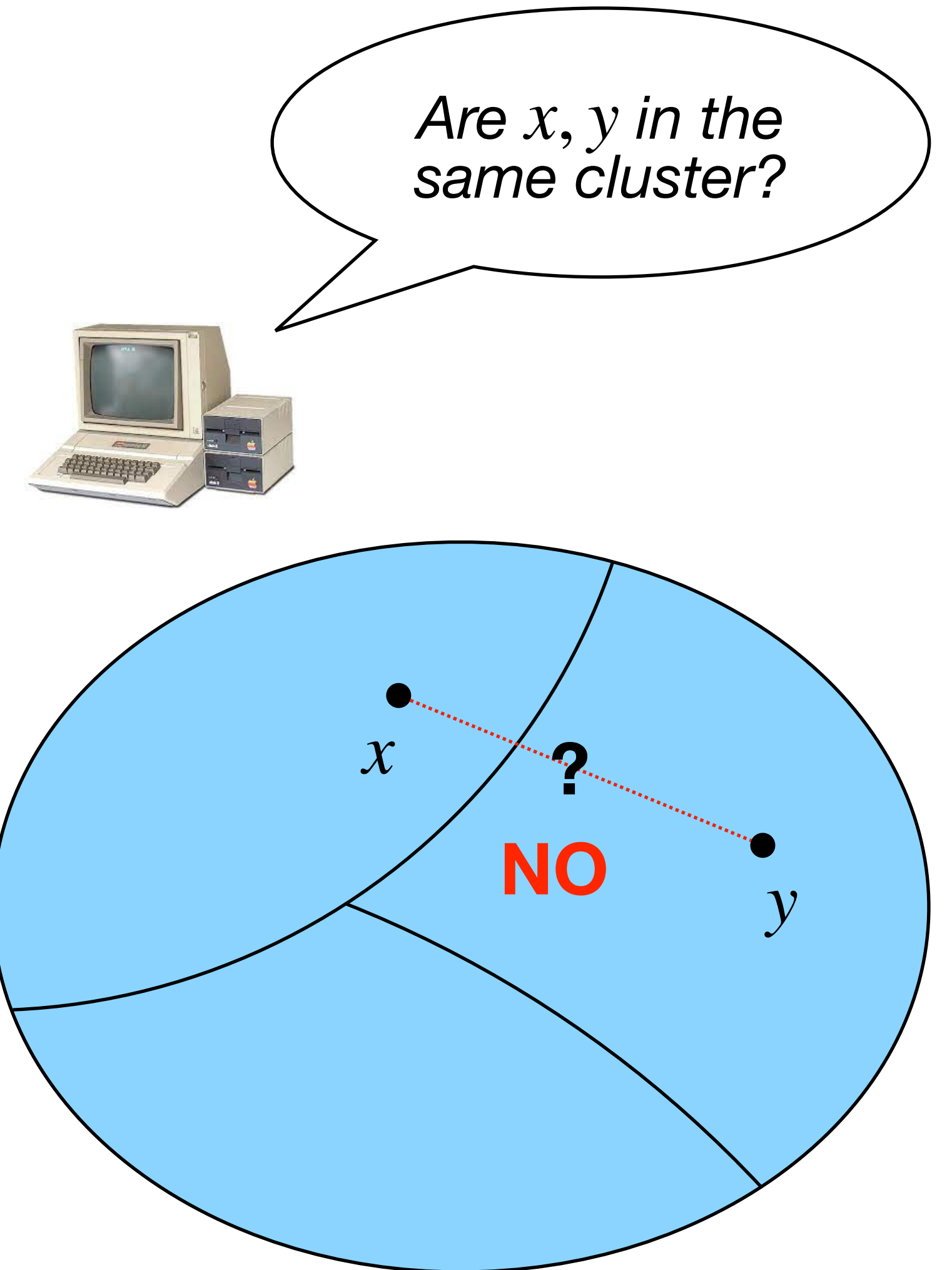
Question: How many queries to learn C_1, \dots, C_k exactly?

Simple **adaptive** $O(nk)$ query algorithm ($k - 1$ rounds), **but...**

Theorem (MS 17, BLMS 24)

Non-adaptive algorithms require $\Omega(n^2)$ queries even for $k = 3$

$O(n^2)$ is trivial



Clustering via Subset Queries

Chakrabarty-Liao [FSTTCS 24], Vinayak-Hassibi [NeurIPS 16] (considered triangle queries)

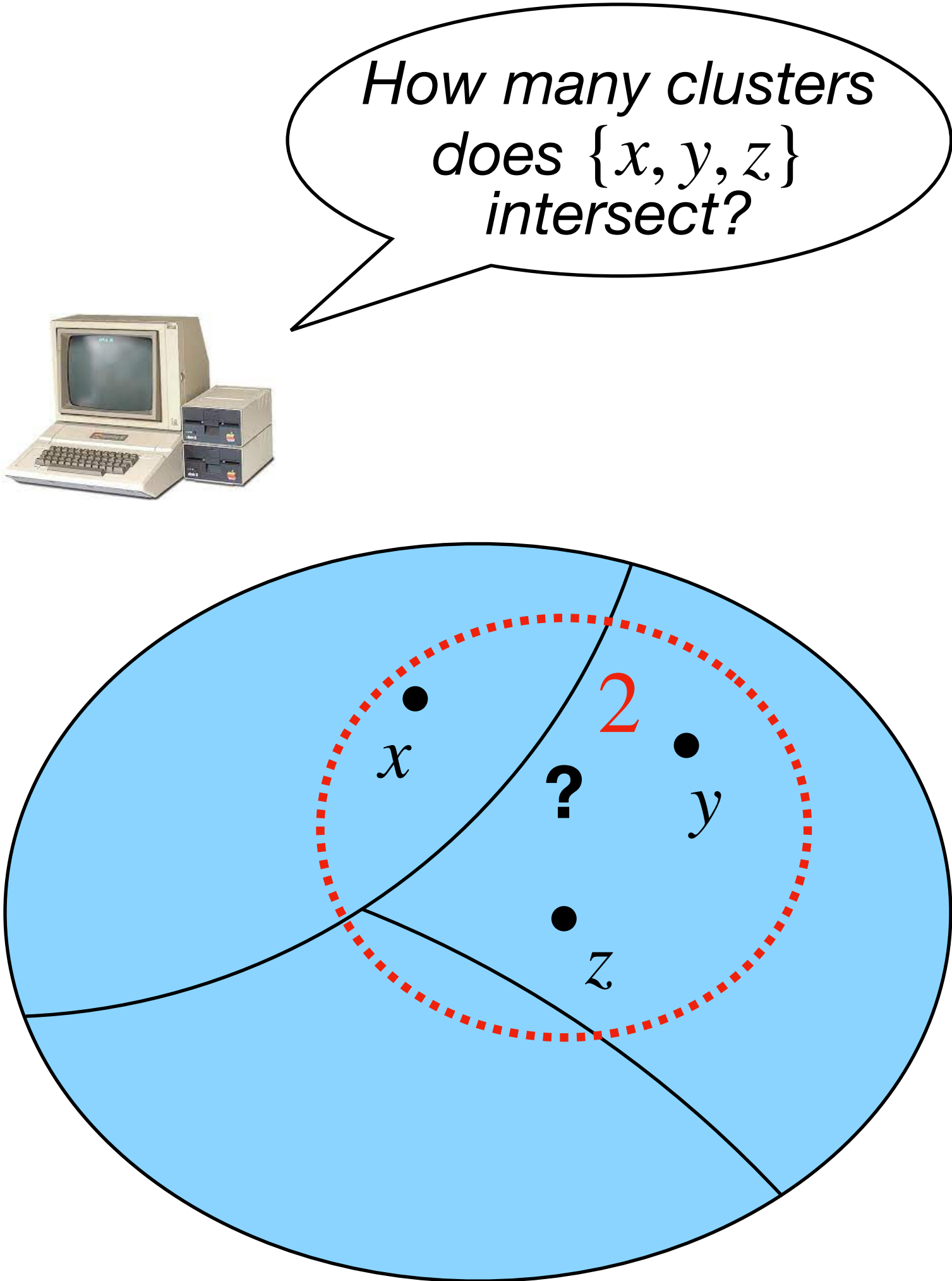
- Set U of n points with hidden partition $C_1 \sqcup \dots \sqcup C_k = U$
 - Can **query** any $S \subseteq U$ and oracle returns $\# j: S \cap C_j \neq \emptyset$
- Question:** How many queries to learn C_1, \dots, C_k exactly?

Information-theoretic lower bound:
 $\Omega(n)$

bits per query: $O(\log k)$
partitions: k^n

Theorem
(Chakrabarty-Liao 24)
 $O(n)$ adaptive algorithm

Questions
How close to linear can we get non-adaptively?
How small of queries can we get away with?



Some of our Results

(all algorithms and lower bounds are non-adaptive)

Unbounded subset queries

Theorem

$O(n \log \log n)$ for $k = O(1)$
 $O(n \log k) + \tilde{O}(k)$ for **balanced** clustering

Question

Is $O(n)$ for $k = 3$ possible using non-adaptive algorithms?

Subset queries of size $|S| \leq s$

Theorem

$O(n \log n \log \log n)$ for $s = O(\sqrt{n}), k = O(1)$
Getting near-linear requires $s = \Omega(\sqrt{n})$

Question

Can we get near-linear with $s = O(\sqrt{n})$ for all k ?

Thank you!