

Watermarking Makes Language Models **Radioactive**

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Motivation

LLM post-training

- Requires a lot of high quality annotations and tricks → 🧠 and 💰
- Practitioners train on data output by a model (e.g., GPT4) → **IP issues**



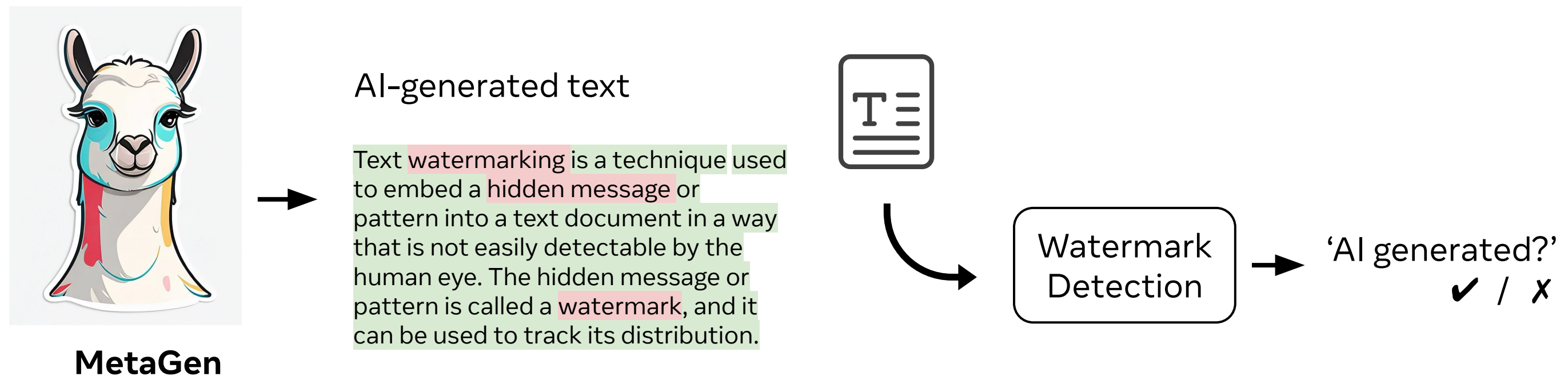
Detection Problem

"Did Bob train on outputs from Alice's model?" is a **very difficult question**



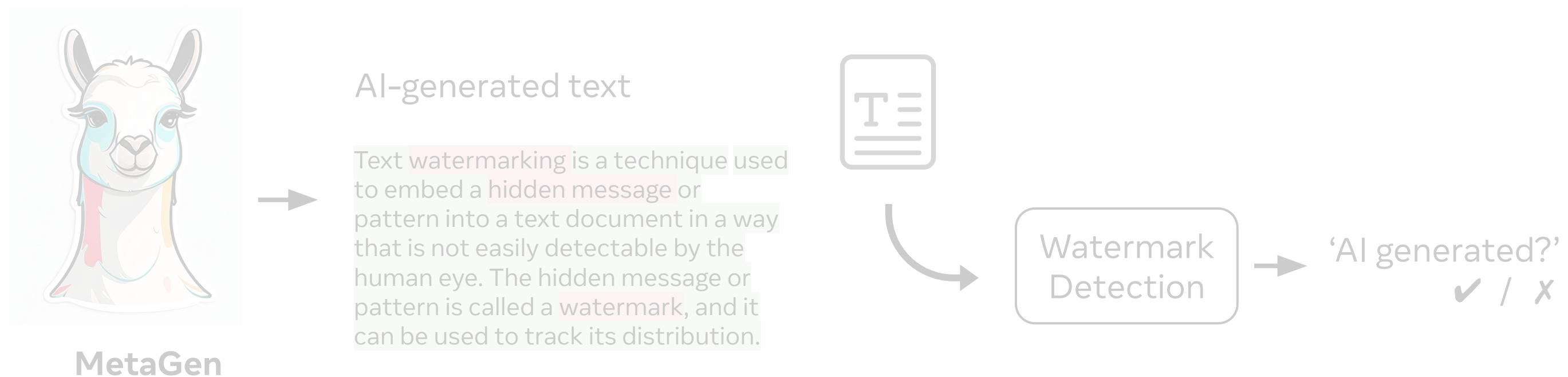
Could Watermarking Give the Answer?

- Watermarking LLMs outputs \approx free lunch
 - Keeps **quality** of the generated text
 - Greatly improves **detection**



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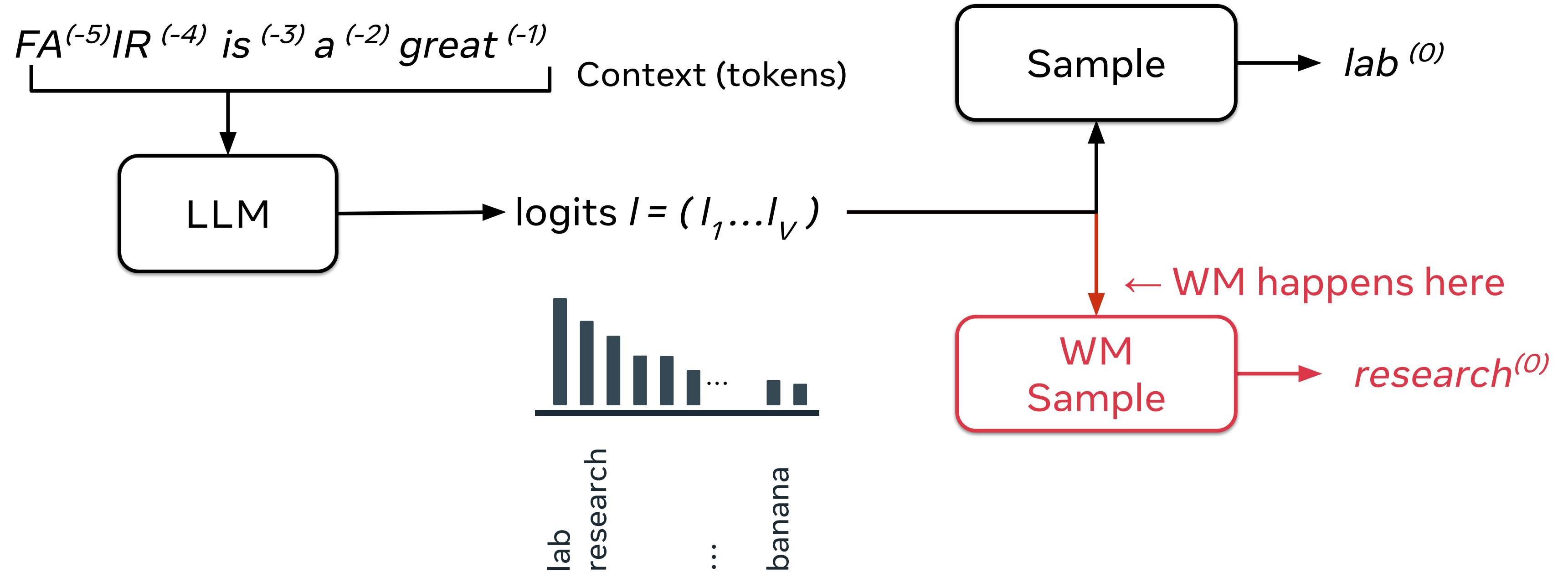


→ “What occurs when we fine-tune an LLM on watermarked data?”

LLM Watermarking 101

Watermarking for LLMs

Generation with LLMs



First Example - Kirchenbauer et al.

 Kirchenbauer et al., *A Watermark for Large Language Models*, ICML 2023

Prompt	Num tokens	Z-score	p-value
...The watermark detection algorithm can be made public, enabling third parties (e.g., social media platforms) to run it themselves, or it can be kept private and run behind an API. We seek a watermark with the following properties:			
No watermark Extremely efficient on average term lengths and word frequencies on synthetic, microamount text (as little as 25 words) Very small and low-resource key/hash (e.g., 140 bits per key is sufficient for 99.999999999% of the Synthetic Internet)	56	.31	.38
With watermark - minimal marginal probability for a detection attempt. - Good speech frequency and energy rate reduction. - messages indiscernible to humans. - easy for humans to verify.	36	7.4	6e-14

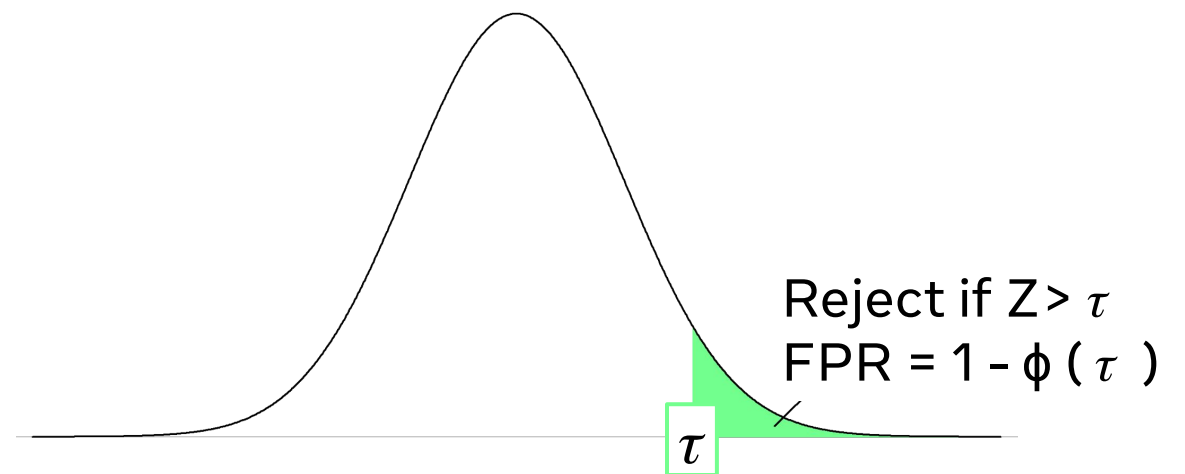
Count Greenlist/Redlist Tokens

Without Watermark	<p>Research on human aggression has been going on for decades, and has been done in a variety of ways. There is no single way to answer this question, and it will depend on the research method and the research question. Humans go to war to protect or expand their territories, and this often results in violence and death. Some argue that war is a natural part of humanity and cannot be eliminated, but this is a controversial view. Human violence has not always</p>	<p>Green: 44 / 91</p> <p>Human/Unwatermarked</p>
With Watermark	<p>To see if they have the stomach to kill another human, and to see if they have the stomach to kill another living thing and risk their life. I'm not saying that justifies it, but those are the reasons. "They had the stomach to kill another human" That's not very nice. They have to kill to survive, so they have to kill someone to kill another person. They don't HAVE TO kill to survive. There are other methods of getting food other than killing. Humans invented agriculture</p>	<p>Green: 73 / 99</p> <p>Watermarked</p>

<https://www.kdnuggets.com/2023/03/watermarking-help-mitigate-potential-risks-lms.html>

Statistical test

- Total score $S = \sum_{t \in 1, \dots, T} S_t =$ number of greenlist tokens
- $H_0 =$ "text is not watermarked"
- Reject based H_0 on Z-Score: $Z = (S - \mu) / \sigma = (S - T/2) / T/4$



How to Choose Greenlist/Redlist?

X Fixed lists

→ heavily biases the generation

lab	Red
research	Green
France	Red
water	Red
mark	Green
FA	Green
IR	Red
word	Red
...	

⇔ “Generate a text on France without using the word France”

How to Choose Greenlist/Redlist?

✗ Fixed lists

→ heavily biases the generation

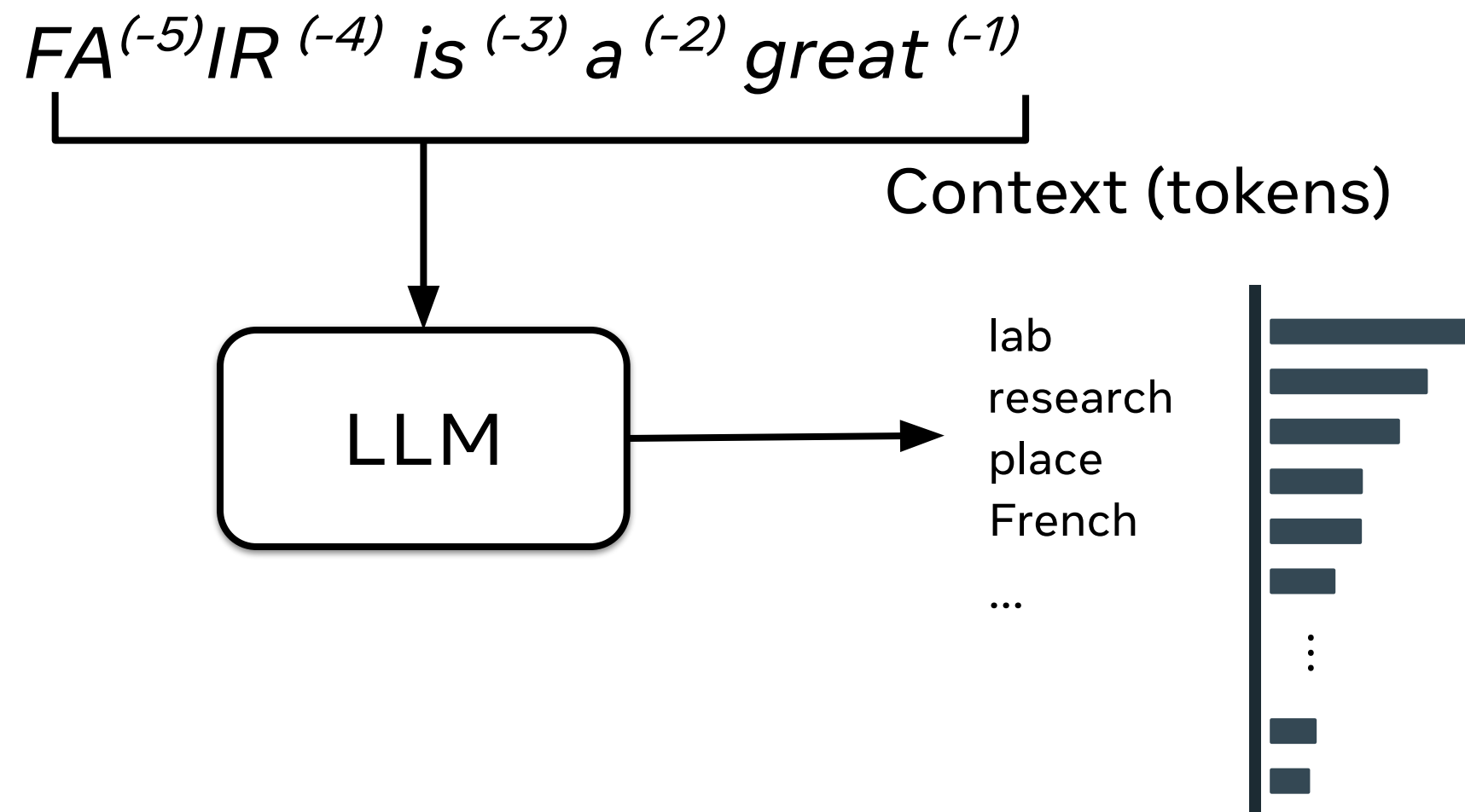
lab	■
research	■
France	■
water	■
mark	■
FA	■
IR	■
word	■
...	

✓ Make it dependant on previous tokens

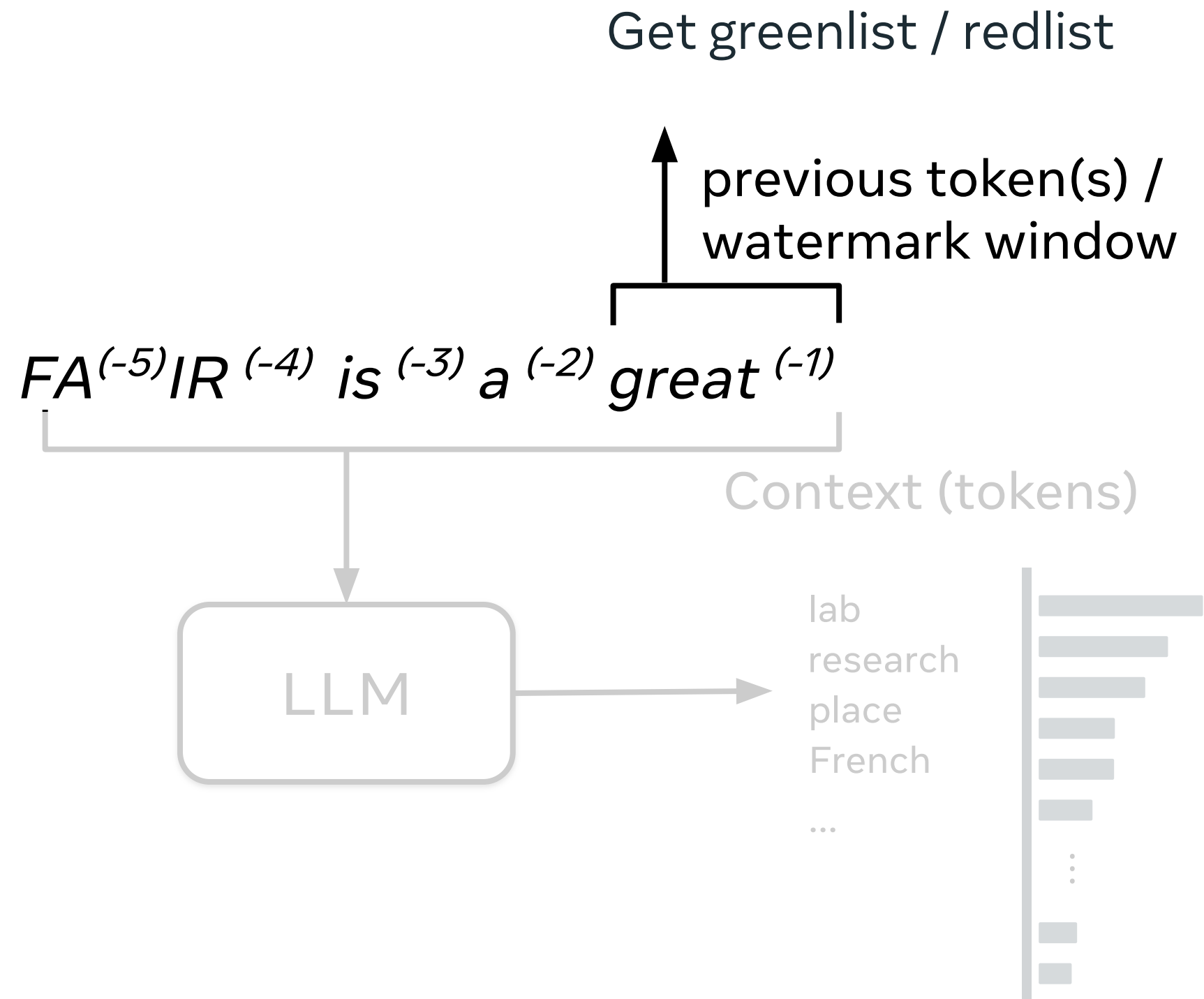
“After word ‘water’, greenlist/redlist are ...”

	lab	research	France	water	mark	FA	IR	word	...
water	■	■	■	■	■	■	■	■	
research	■	■	■	■	■	■	■	■	
France	■	■	■	■	■	■	■	■	
water	■	■	■	■	■	■	■	■	
mark	■	■	■	■	■	■	■	■	...
FA	■	■	■	■	■	■	■	■	
IR	■	■	■	■	■	■	■	■	
word	■	■	■	■	■	■	■	■	

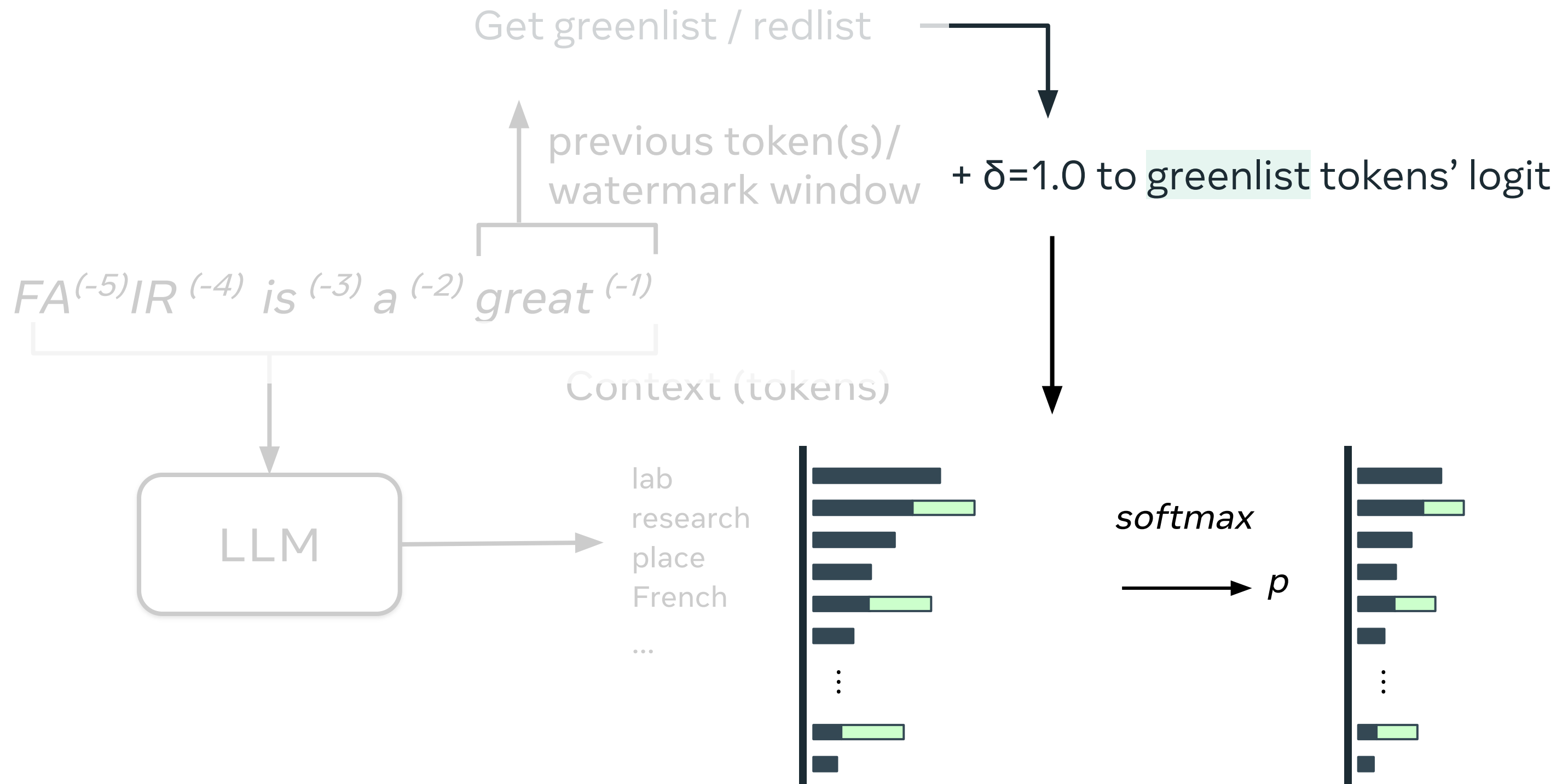
Sampling with Greenlist/Redlist



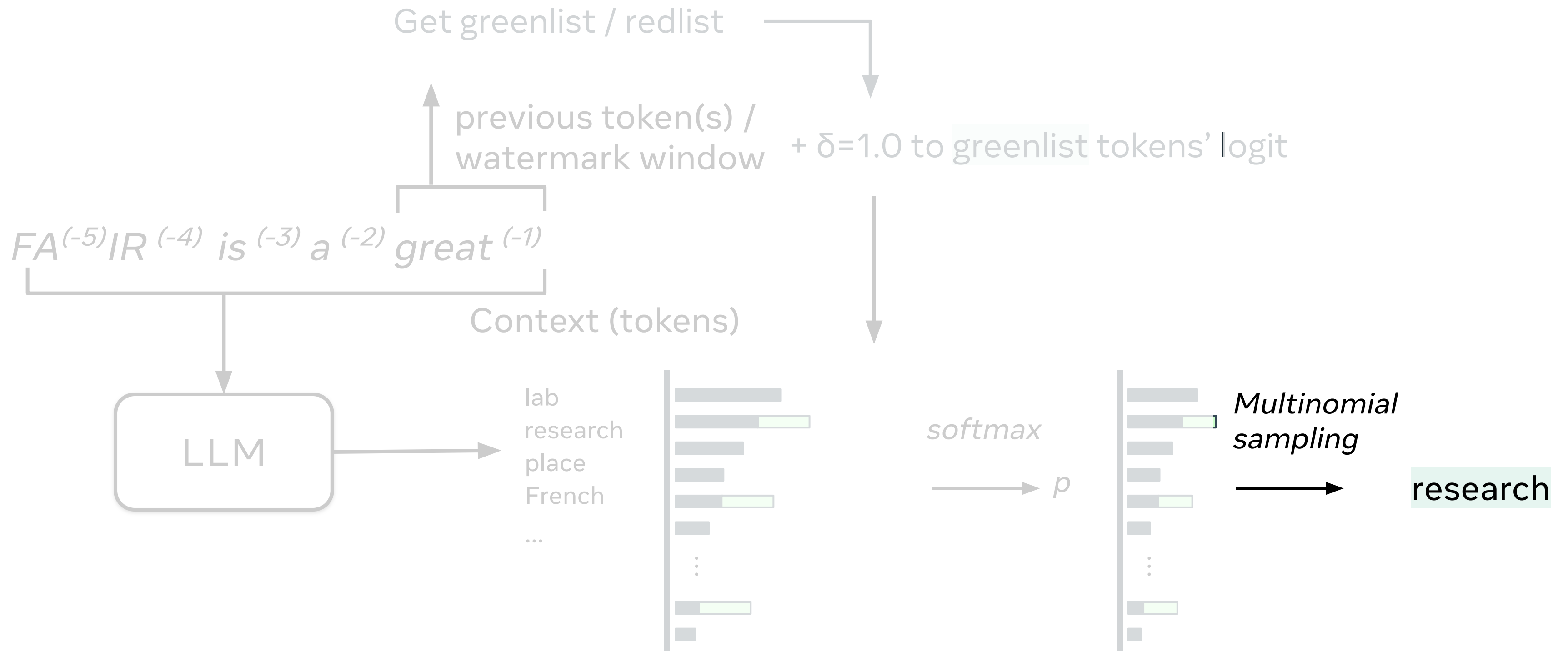
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Sampling with Greenlist/Redlist

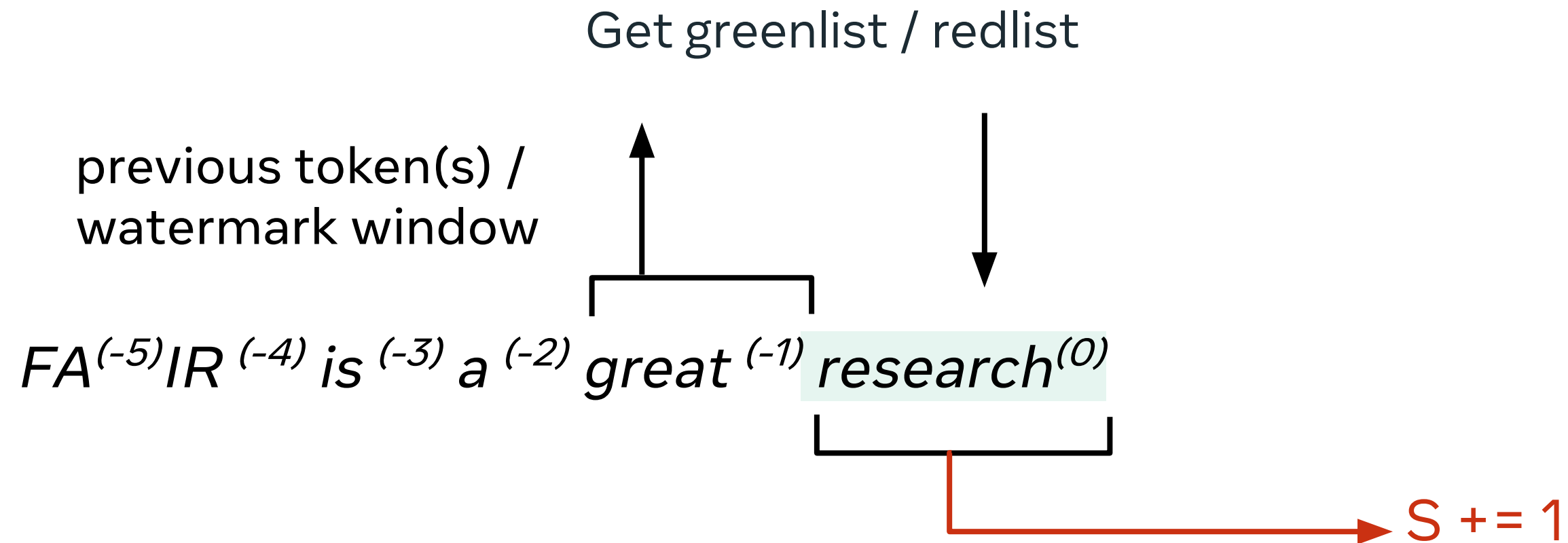


Sampling with Greenlist/Redlist



Detection with Greenlist/Redlist

Compute score



Statistical test

- Total score $S = \sum_{t \in 1, \dots, T} S_t =$ number of greenlist tokens
- $H_0 =$ "text is not watermarked"
- Reject based H_0 on Z-Score: $Z = (S - \mu) / \sigma$ or Binomial test

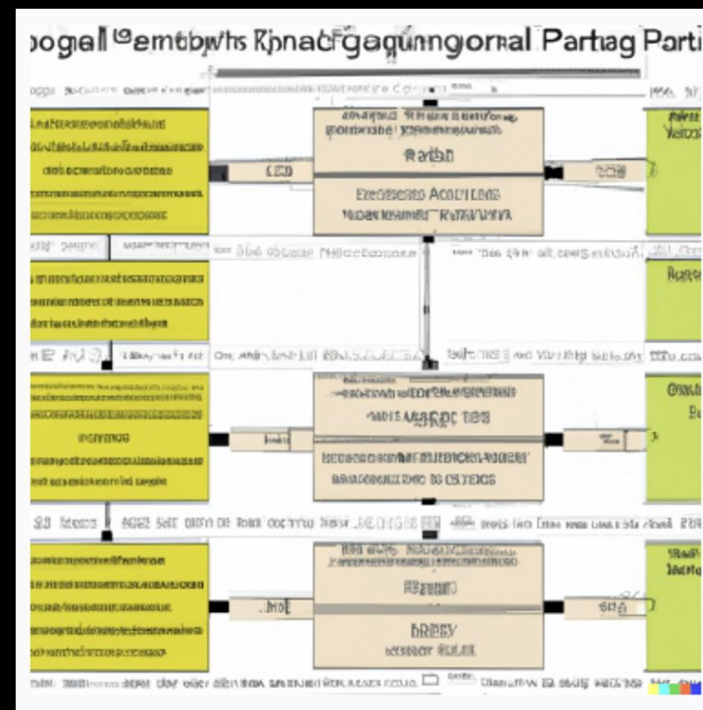
Second Example - Aaronson et al.

 Aaronson et al., *Watermarking GPT Outputs*, 2022

Watermarking GPT Outputs

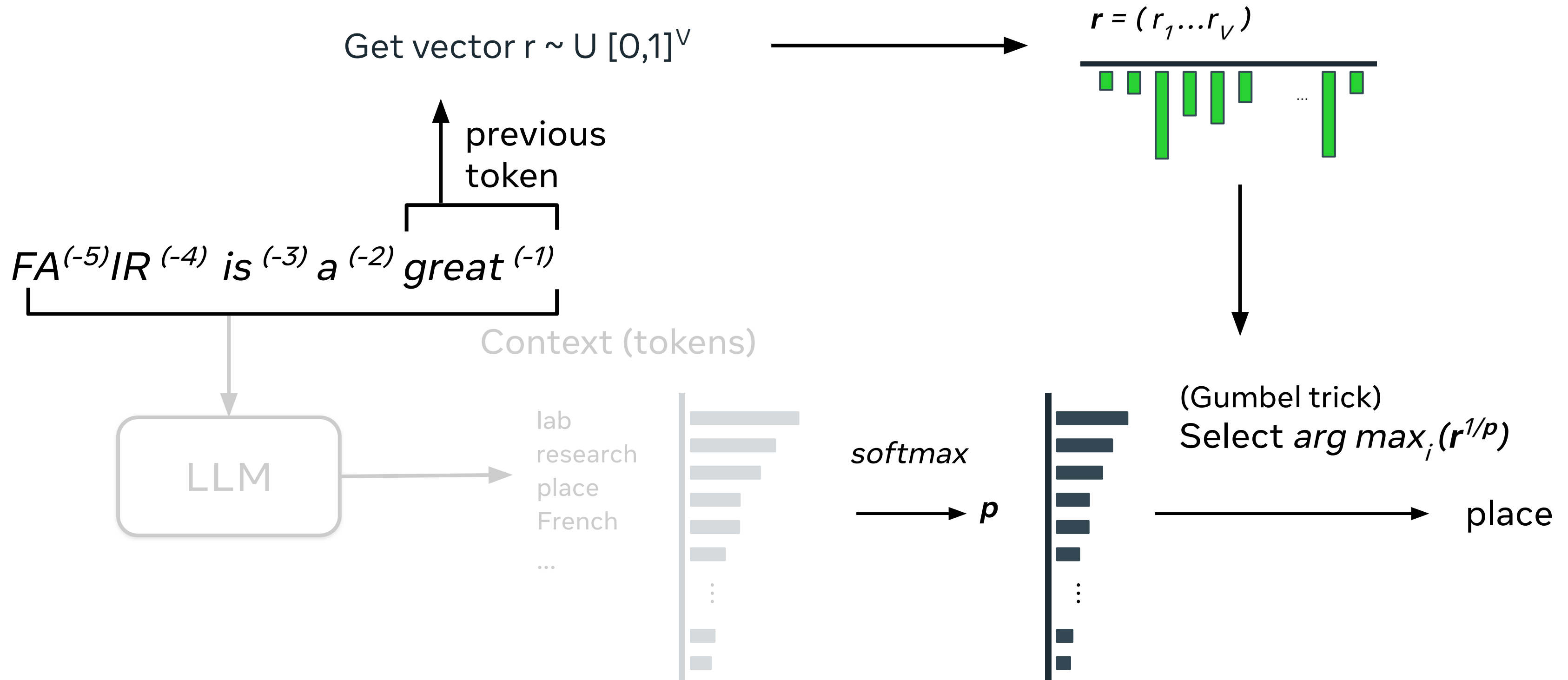
Scott Aaronson (UT Austin and [OpenAI](#))

Joint work with Hendrik Kirchner ([OpenAI](#))



December 13, 2022

Sampling with Gumbel Trick

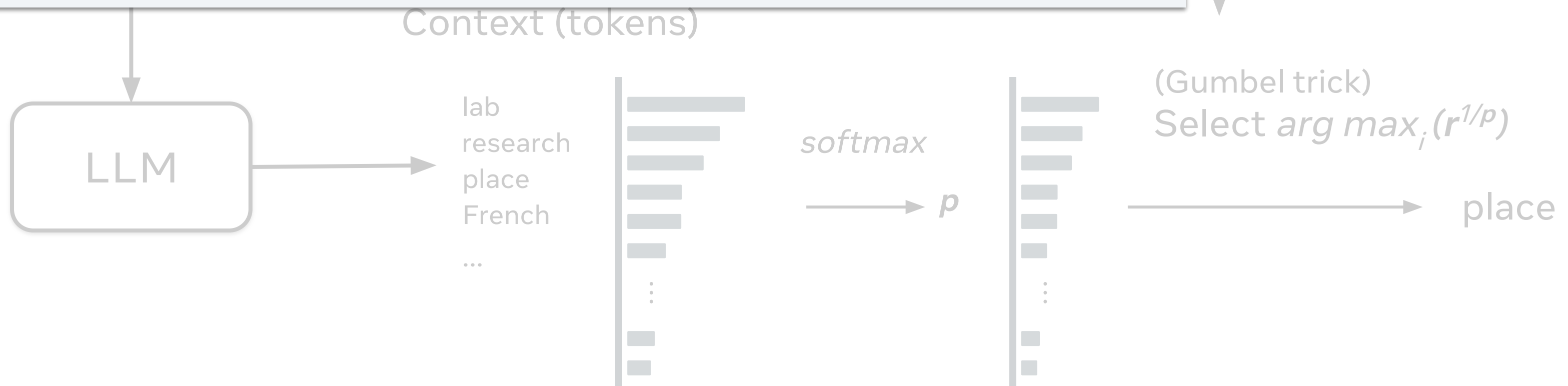
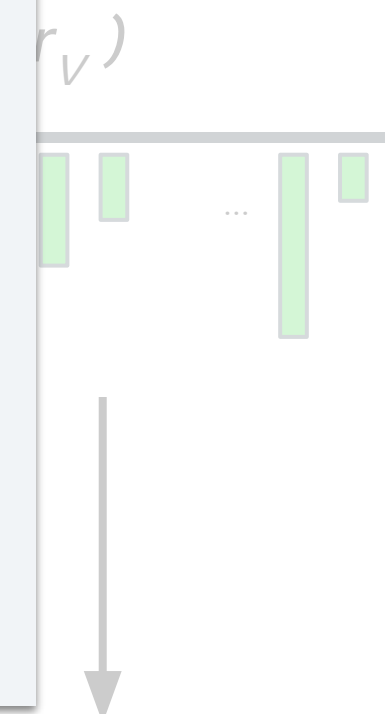


Sampling with Gumbel Trick

Property (Gumbel trick):

$$\forall i \in [1, \dots, V], P \left(\arg \max_i R_i^{1/p_i} = i \mid R \sim U(0, 1)^V \right) = p_i$$

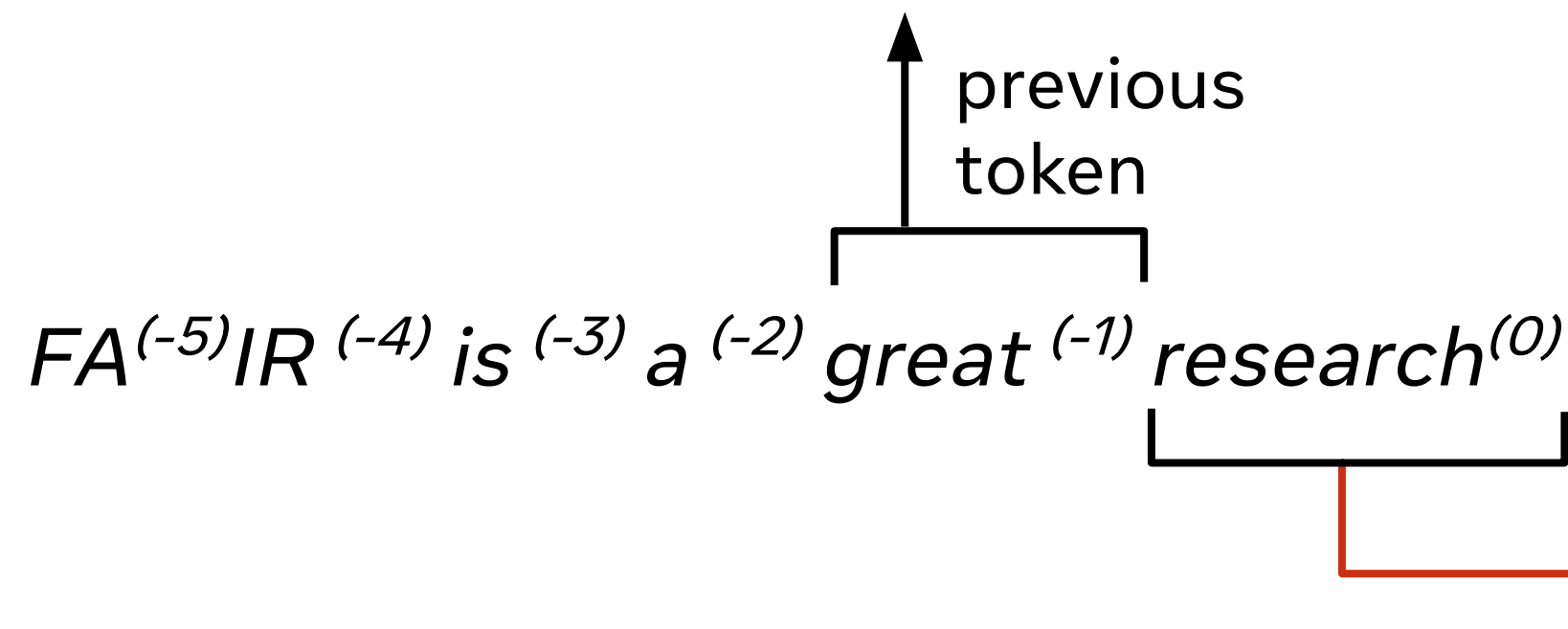
→ “**Proba of choosing token i is p_i** ”



Detection with Z-score

Compute score

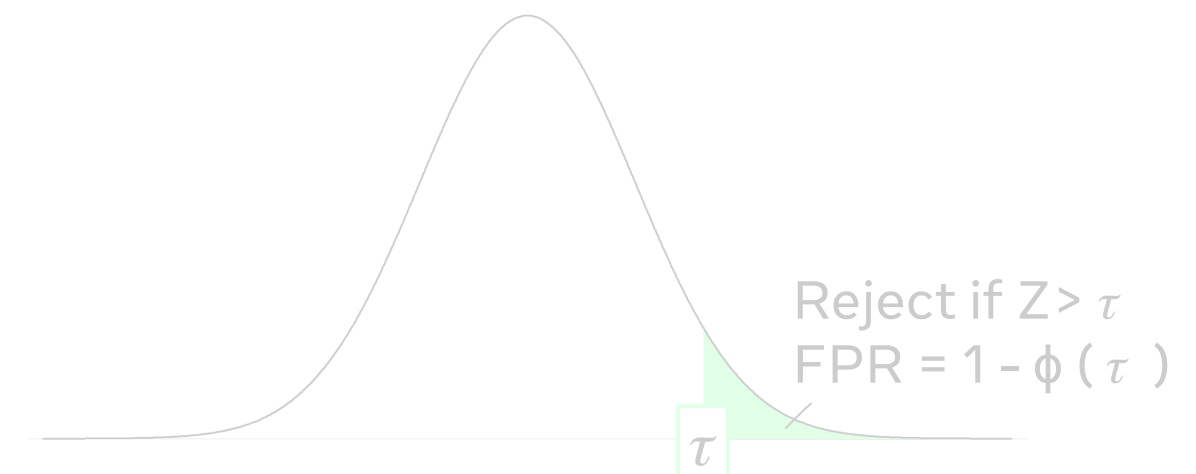
Get vector $r \sim U [0,1]^V$



Score increment:
 $-\ln(1-r_t)$ with t the index of chosen token

Statistical test

- Total score $S = \sum_{t \in 1, \dots, T} S_t$
- H_0 = "text is genuine" - H_1 = "text is watermarked"
- Reject based H_0 on Z-Score: $Z = (S - \mu) / \sigma$



Detection with Z-score

Compute score

Get vector $r \sim U [0,1]^V$

↑ previous

Property:

(H_0) For non-watermarked texts: $\mathbb{E}(S_T) = T$

(H_1) For watermarked texts: $\mathbb{E}(S_T) \geq T + \left(\frac{\pi^2}{6} - 1 \right) H_T$

Sta

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Reject if $Z > \tau$
FPR = $1 - \phi(\tau)$

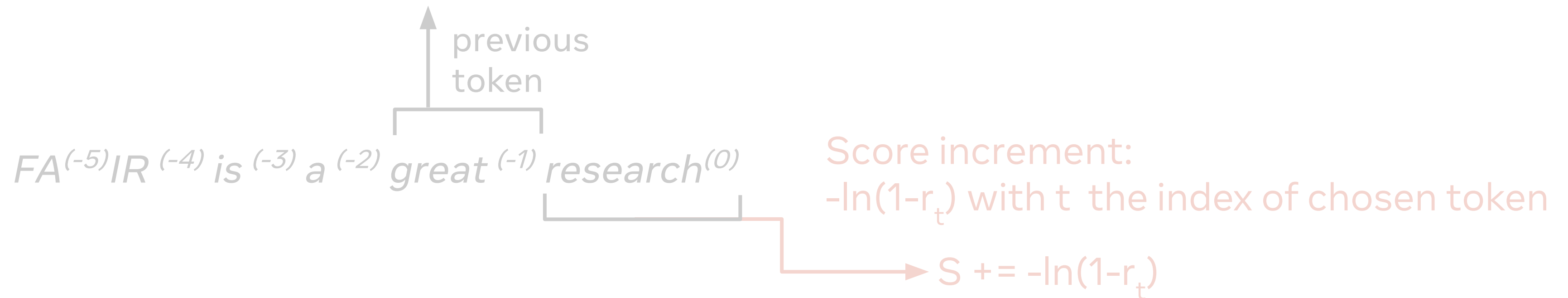
τ

osen token

Detection with Z-score

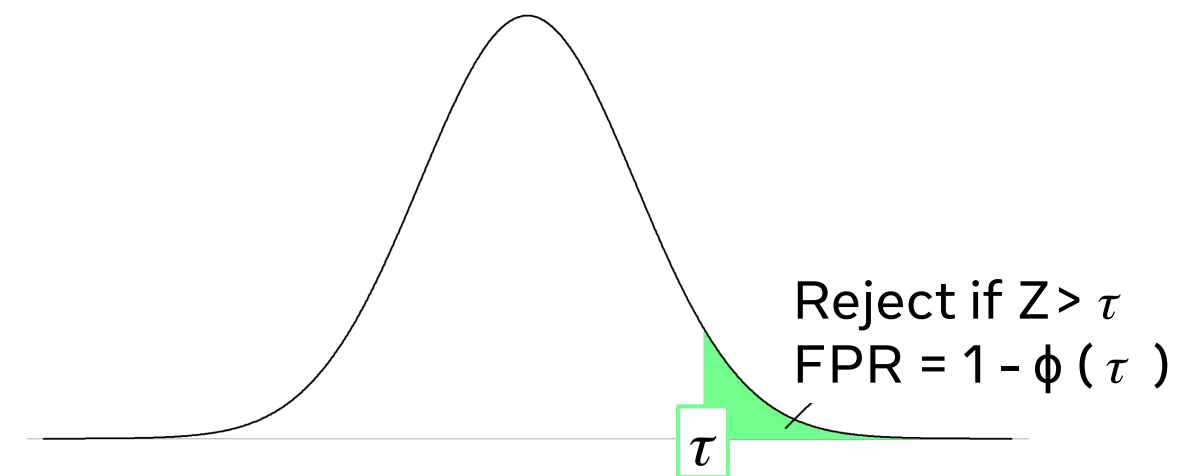
Compute score

Get vector $r \sim U [0,1]^V$



Statistical test

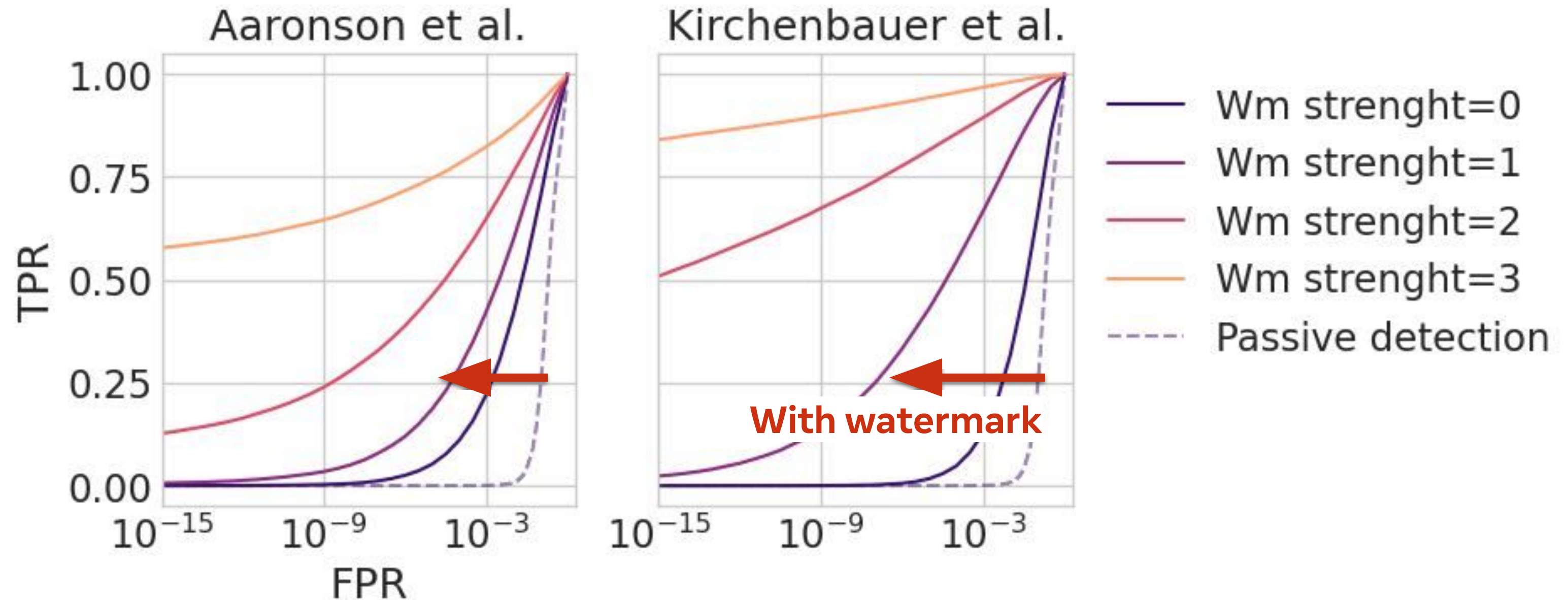
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Example - Detection Results

10k positive AI-generated texts (from OpenAssistant Conversations dataset)

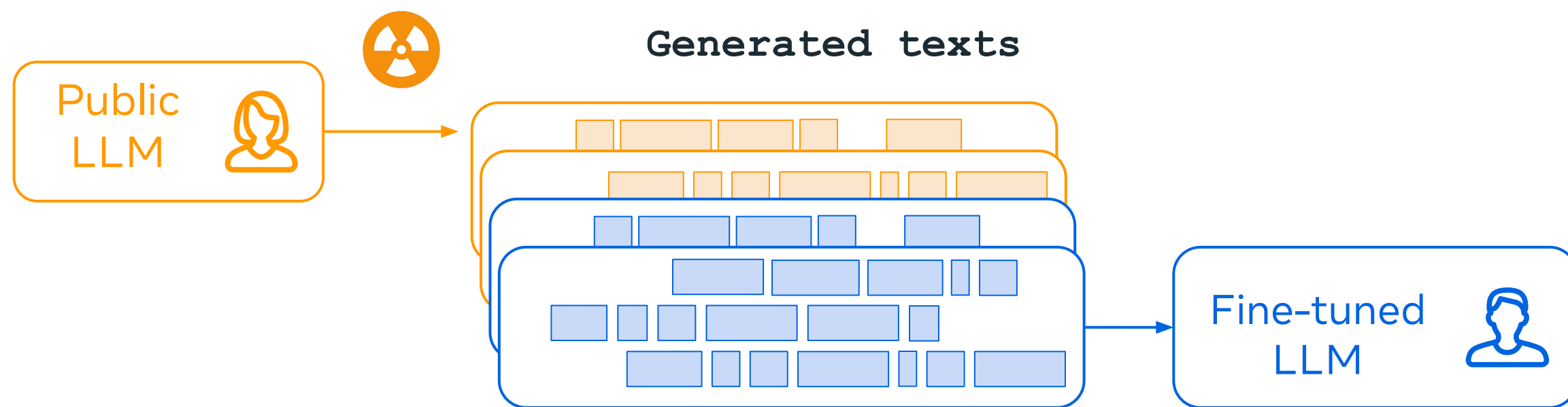
Passive detection ↔ DetectGPT [[Mitchell, Eric, Yoonho Lee, Alexander Khazatsky, Christopher D. Manning, and Chelsea Finn. "Detectgpt: Zero-shot machine-generated text detection using probability curvature.", ICML 2023](#)]



Radioactivity

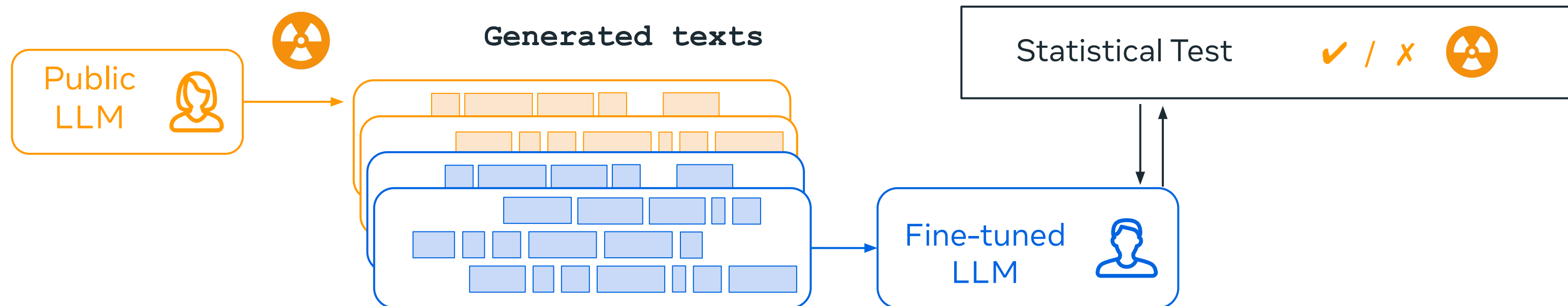
Problem under Study

- Bob fine-tunes his LLM on **training data** with a small proportion of texts coming from Alice's LLM.



Problem under Study

- Bob **fine-tunes** his LLM on **training data** with a small proportion of texts coming from **Alice's LLM**.
- Alice wants to know if Bob has **fine-tuned on outputs from her model**



Radioactivity

Definition: Radioactivity refers to the possibility for Alice to detect with statistical evidence that Bob fine-tuned on outputs from her model

More rigorously,

Definition 1 (Text Radioactivity). *Dataset D is α -radioactive for a statistical test T if “ \mathcal{B} was not trained on D ” $\subset \mathcal{H}_0$ and T is able to reject \mathcal{H}_0 at a significance level (p-value) smaller than α .*

Definition 2 (Model Radioactivity). *Model A is α -radioactive for a statistical test T if “ \mathcal{B} was not trained on outputs of A ” $\subset \mathcal{H}_0$ and T is able to reject \mathcal{H}_0 at a significance level smaller than α .*

Different Settings

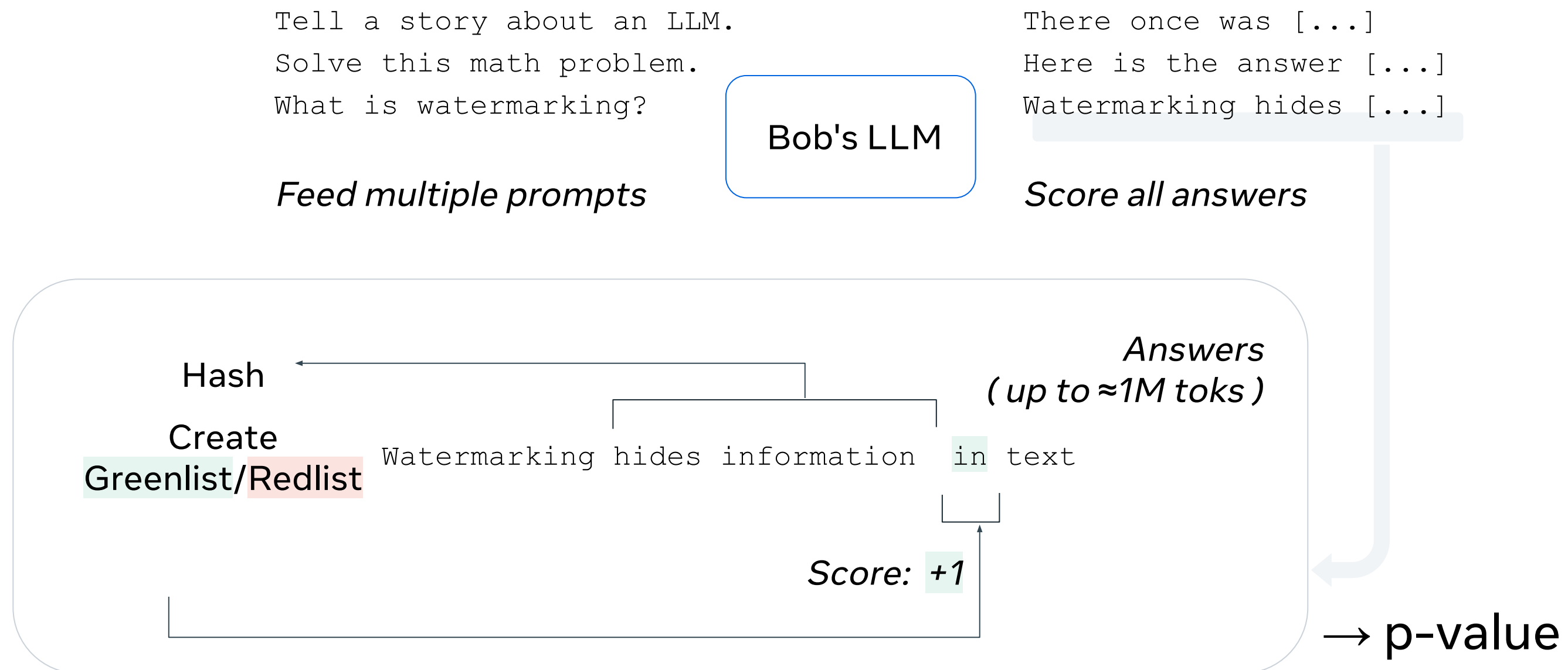
		Model access	
		Model is open (Mistral, Llama, Gemma, etc.)	API access only (GPT, Claude, etc.)
Data access	Access to the text used by Bob (GPT, Claude, etc.)	Open / Supervised	Closed / Supervised
	Text used by Bob is unknown (Llama, API but obfuscation of user)	Open/ Unsupervised	Closed/ Unsupervised

Radioactivity detection availability from other methods in the literature

	With WM		Without WM (MIA)		IPP	
	Open	Closed	Open	Closed	Open	Closed
Supervised	✓	✓	✓	✗	✓	~
Unsupervised	✓	✓	✗	✗	✗	✗

Naive Approach for Radioactivity Detection with Watermarking

Prompt the model, get many output tokens, get the score and the p-value of the WM detection



Problems with the Naive Approach

Watermark signal is weak

→ hard to get p-values $< 10^{-1}$ for low proportions of watermarked data in the training set

p-values break down when too many tokens are scored

→ when scoring too many tokens, the detection test gives very low p-values even for LLMs trained without watermarked text, so the statistical tests are inaccurate

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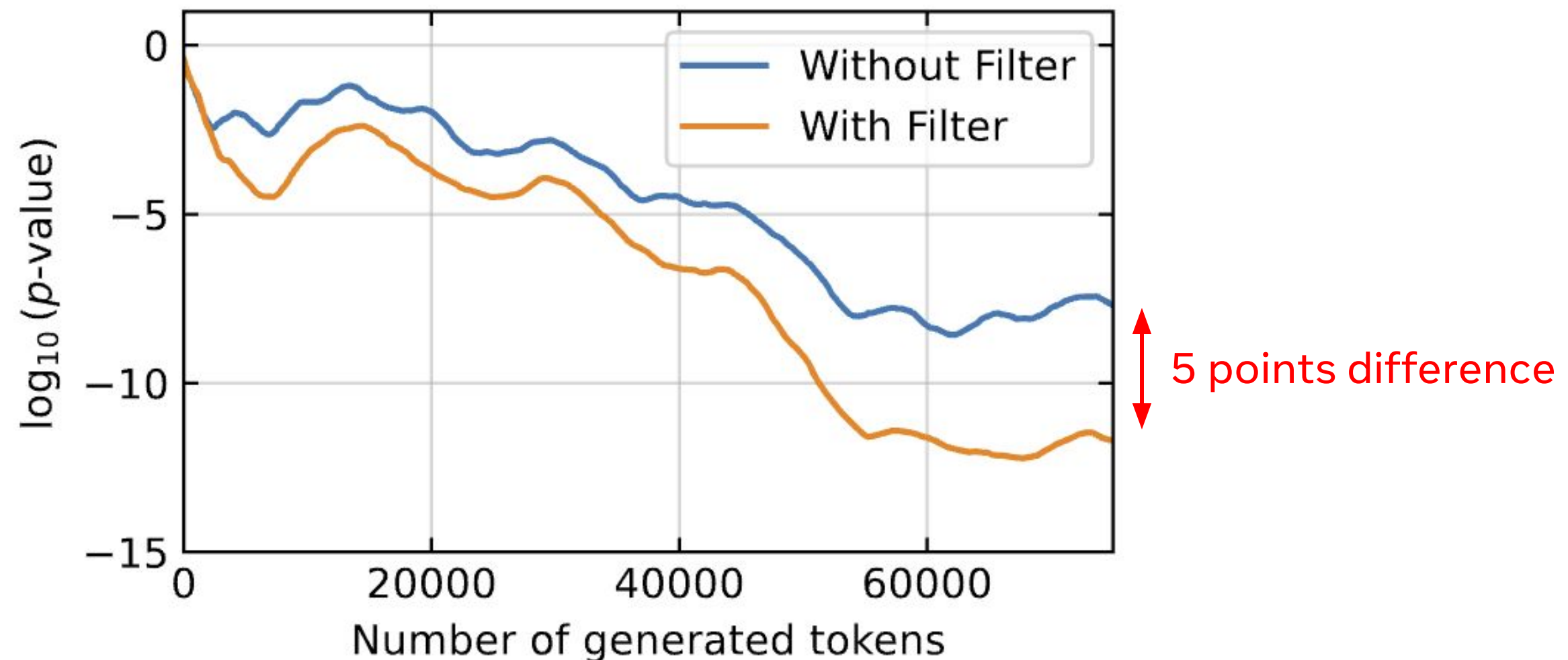
Improvements

- Leverage access to the data
- Leverage access to the model
- While keeping accurate p-values through deduplication

Trick 1: Filter

Radioactivity can only be detected on watermark windows present in training

- **Supervised setting:** only score watermark windows suspected to be part of training
- **Unsupervised setting:** see what are the watermark windows that are most often produced by the watermark, and only score these



Trick 2: Choose the Good Input

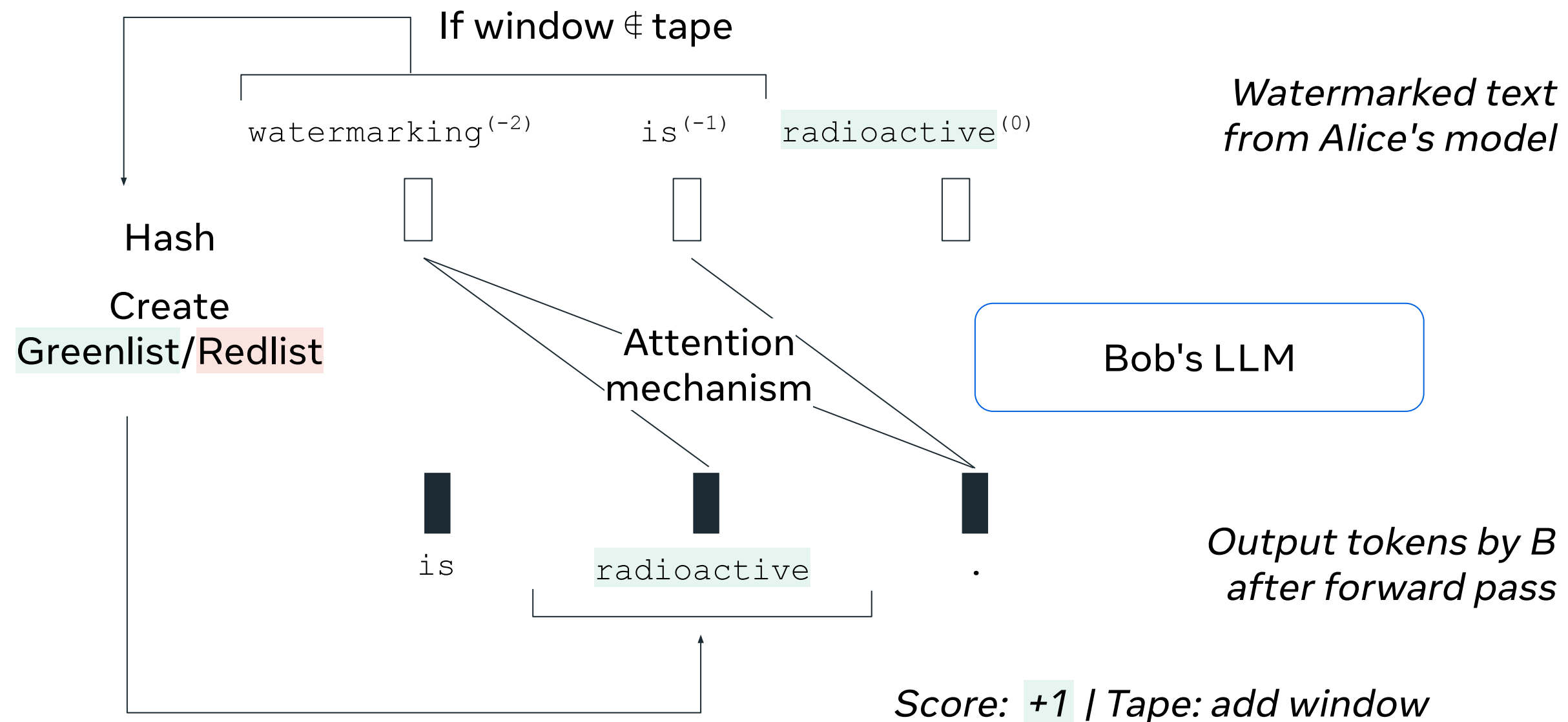
Radioactivity can only be detected on k-grams that were present in training

- **Closed-model:** Alice prompts Bob's model with questions that she thinks were used
- **Open-model:** Alice "reads" the data that she thinks Bob has used

Trick 3: Open Model

When access to the model is given, Alice can forward text directly to the model

- **Gain in efficiency:** one pass forward only
- **Gain in supervision:** the model sees exact reproduction of watermark window & context



Trick 4: Deduplication for False Positives

- Very important to get reliable p-values

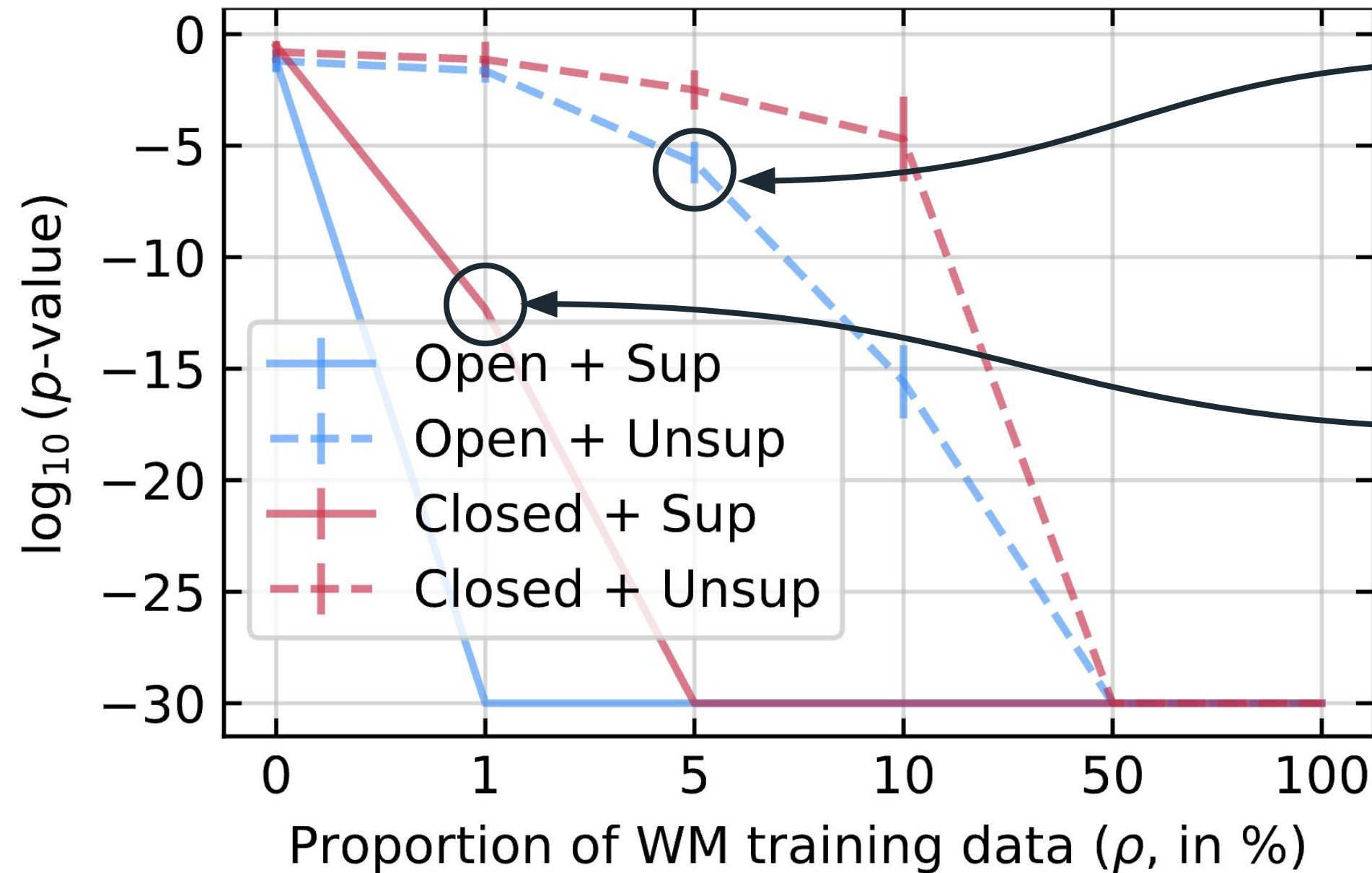
Access to Model	De-duplication	
	With	Without
Open	0.46 ± 0.27	0.053 ± 0.12
Closed	0.42 ± 0.30	$< 10^{-30}$

- Lots of rules:
 - Don't score tokens whose watermark window have already been scored
 - Don't score tokens whose watermark window is already in the attention span

Experimental Setup

1. Generate watermarked instructions with Llama-2-chat-7b and Self-Instruct
2. Fine-tune Llama-1-7b with varying proportions of watermarked instructions
3. Get p-values of radioactivity detection

Detection Results under the Different Settings



- if the suspect model is open-weight, detection has p-value $< 10^{-5}$ even when as little as 5% of training text is watermarked

- when Alice only has API access but knows which data have been used, detection has p-value $< 10^{-10}$ even when 1% of the training text is watermarked

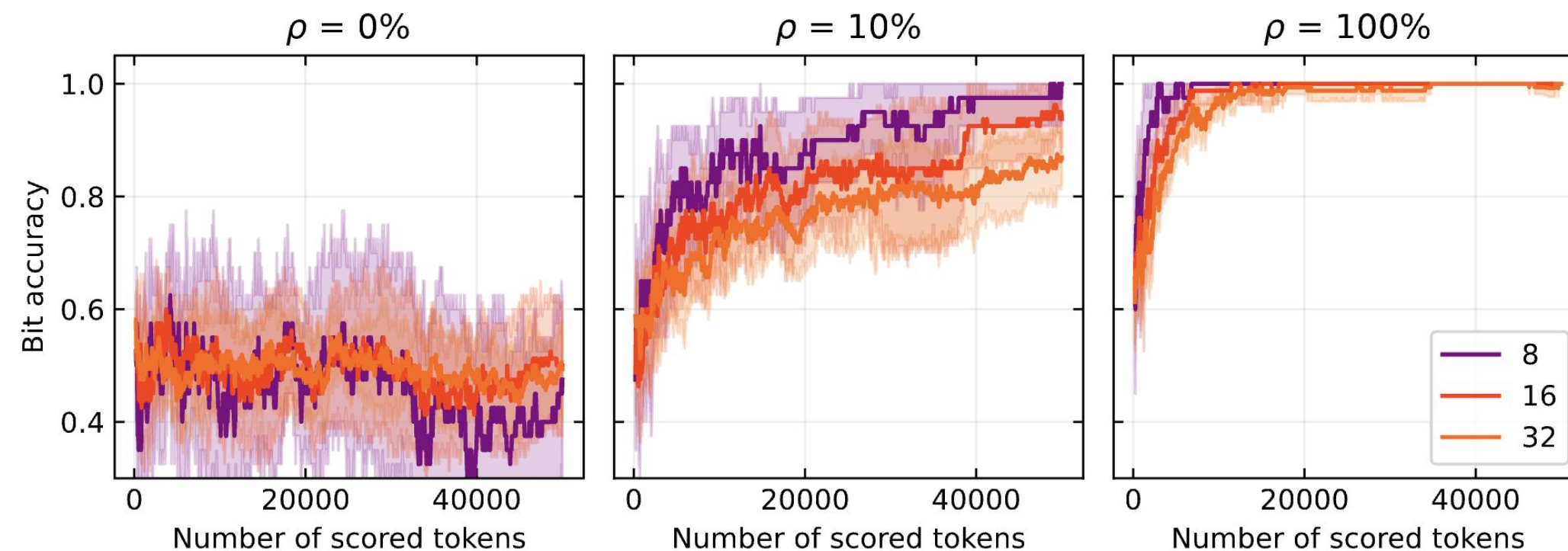
Ablations

Post-training optimization has a big influence on radioactivity

\log_{10} p-value for 10k observed tokens under the supervised-open model setting

(a) Learning rate.			(b) Epoch.				(c) Adapters.		(d) Model size.	
10^{-5}	$5 \cdot 10^{-5}$	10^{-4}	1	2	3	4	Full	Q-LoRA	7B	13B
-32.4	-49.6	-58.0	-20.8	-29.2	-33.2	-34.8	-32.4	-11.0	-32.4	-33.2

The method generalizes to multi-bit watermarking



Ablations

A lot more in the paper!

Main Takeaways

Watermarking makes LLM radioactive:

- Training on watermarked data can be **detected with very high confidence...**
- ... even for **small proportions** of WM data

Thanks!