

Multi-body $SE(3)$ Equivariance for Unsupervised Rigid Segmentation and Motion Estimation

Jia-Xing Zhong, Ta-Ying Cheng, Yuhang He, Kai Lu,
Kaichen Zhou, Andrew Markham, Niki Trigoni

Department of Computer Science, University of Oxford

Presenter: Jia-Xing Zhong

Overview

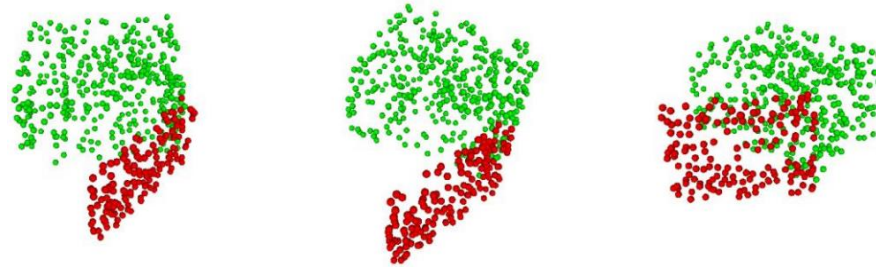
- Problem Statement
- Motivation & Main Idea
- Methodology
- Experiments
- Q & A

Problem Statement

- Unsupervised Multi-body Rigid Segmentation and Motion Estimation

- Input

- A set of K point cloud frames: $P = \{P_1, P_2, \dots, P_{K-1}, P_K\}$



- Unsupervised: No training labels
 - Multi-body: Unknown multiple parts

- Output

- Rigid Segmentation: Moving-part rigid masks.
 - Motion Estimation: Per-part rotations and translations.

Motivation & Main Idea

- Motivation

- Open-set pose changes
 - SE(3)-equivariance
- Category-agnostic about moving part
 - Matching

g : rigid transformation
 f : features
 x : a point in point clouds

- Background

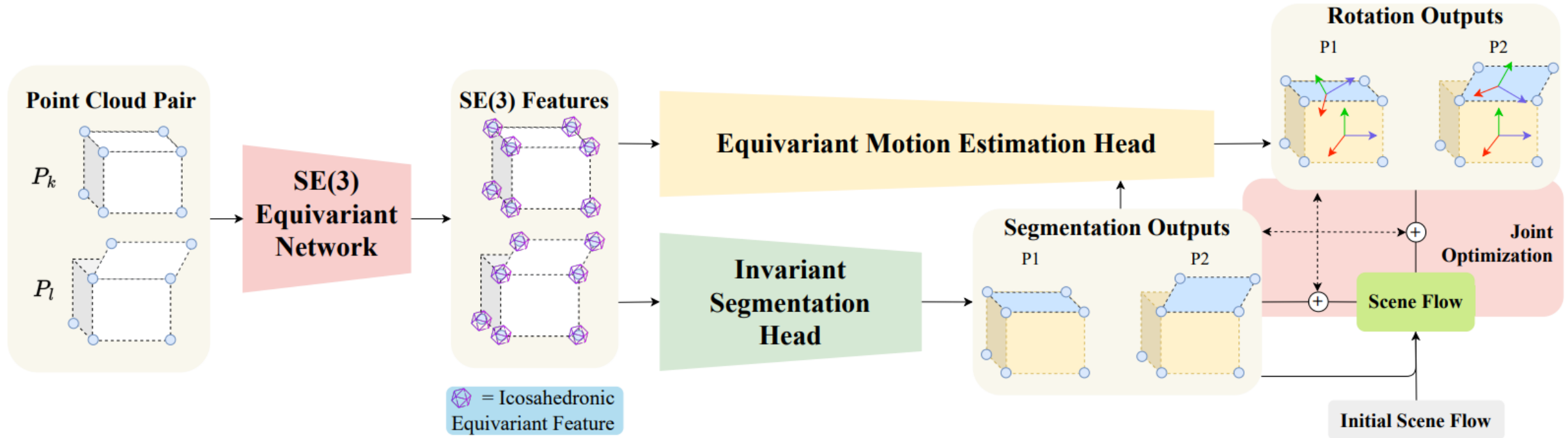
- SE(3)-equivariance

1) Rotation equivariance within the icosahedral group: $f(g \circ x) = g \circ f(x), \forall g \in \mathcal{G}$.
2) Translation invariance w.r.t. arbitrary translation t : $f(t \circ x) = f(x)$.

- Main Idea

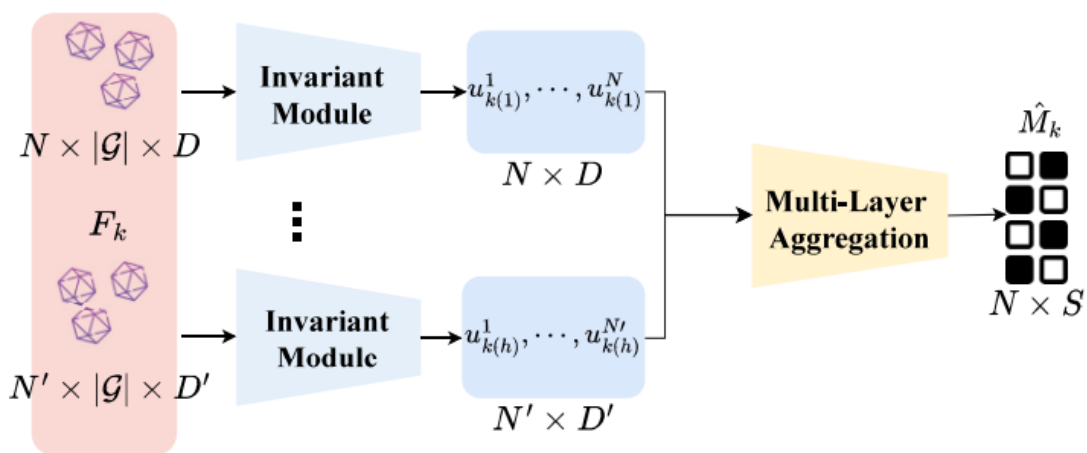
- **Training Strategy:** simultaneously filter out the noisy flow predictions and refine the estimates of rigid motion by exploiting the interrelation among scene flow, segmentation mask, and rigid transformation
- **Architecture:** Category-agnostic part-level SE(3)-equivariance

Methodology

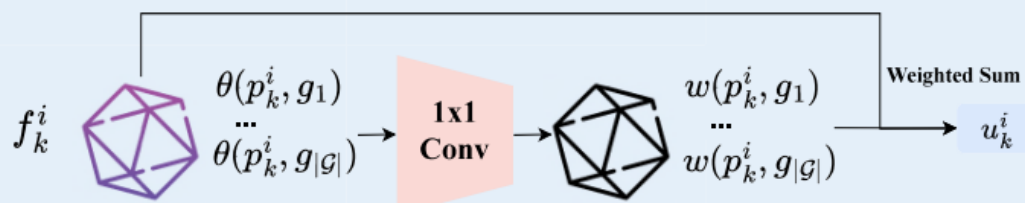


Methodology

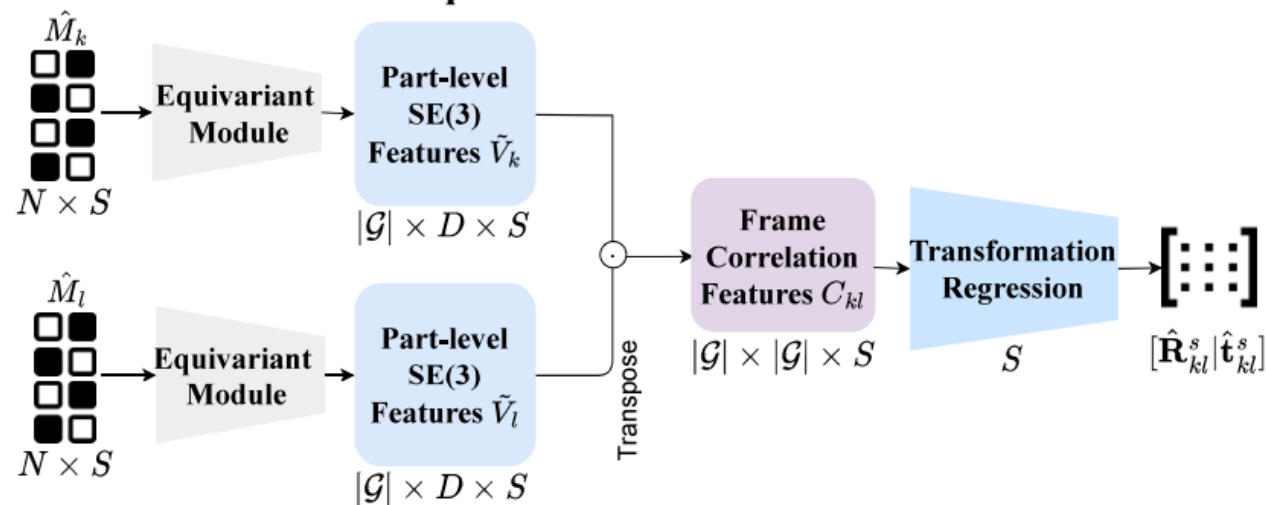
Invariant Segmentation Head



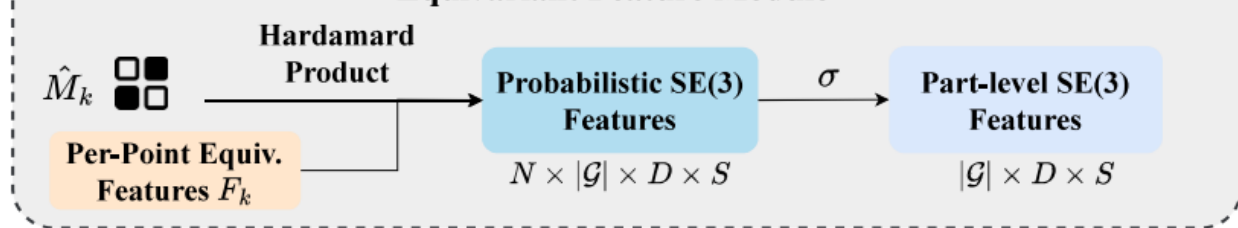
Invariant Module



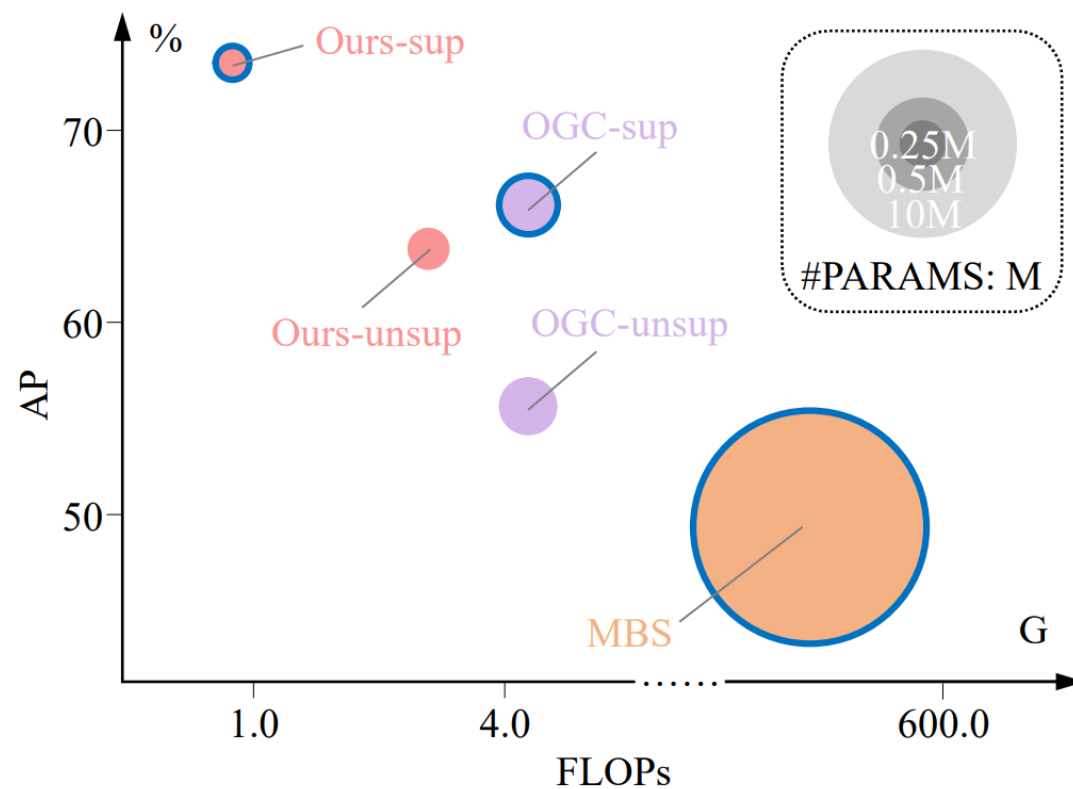
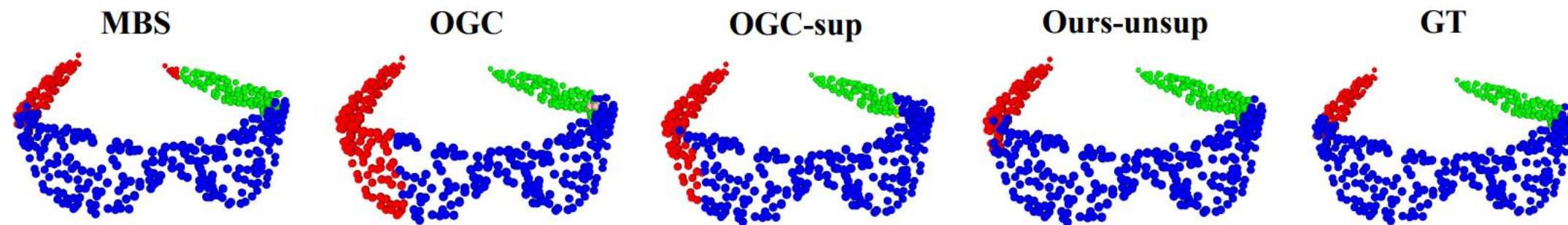
Equivariant Motion Head



Equivariant Feature Module



Experiments



Experiments

Table 1: *Ablation studies on SAPIEN.*

Seg. Head		Scene Flow		Mot. Head	Metrics						
SE(3) Feat.	Point-level Flexibility	Current	Past	Consensus	AP \uparrow	PQ \uparrow	F1 \uparrow	Pre \uparrow	Rec \uparrow	mIoU \uparrow	RI \uparrow
					45.2	44.2	58.9	53.8	65.1	60.9	71.2
✓					51.7	50.0	65.8	64.7	67.0	61.6	72.3
✓	✓				55.3	52.8	68.3	65.9	70.0	62.3	72.7
✓	✓	✓			54.8	52.0	67.6	66.0	69.3	63.5	73.8
✓	✓	✓	✓		57.0	51.6	67.3	63.8	71.1	63.1	73.2
✓	✓	✓	✓	✓	63.8	61.3	77.3	84.2	71.3	63.7	75.4

Experiments

Table 2: *Rigid segmentation and motion estimation results on SAPIEN.* * indicates that we evaluate these metrics upon the officially released model; - means that the metric is unavailable.

		AP \uparrow	PQ \uparrow	F1 \uparrow	Pre \uparrow	Rec \uparrow	mIoU \uparrow	RI \uparrow	EPE3D \downarrow
Supervised Methods	PointNet++ [55]	-	-	-	-	-	51.2	65.0	-
	MeteorNet [46]	-	-	-	-	-	45.7	60.0	-
	DeepPart [71]	-	-	-	-	-	53.0	67.0	5.95
	MBS [32]	49.4*	52.6*	67.6*	61.4*	75.2*	67.3	77.0	5.03
	OGC-sup [61]	66.1	48.7	62.0	54.6	71.7	66.8	77.1	-
	Ours-sup	73.5	57.8	71.1	65.6	77.7	72.6	81.4	3.86
Unsupervised Methods	TrajAffn [52]	6.2	14.7	22.0	16.3	34.0	45.7	60.1	-
	SSC [51]	9.5	20.4	28.2	20.9	43.5	50.6	65.9	-
	WardLinkage [66]	17.4	26.8	40.1	36.9	43.9	49.4	62.2	-
	DBSCAN [19]	6.3	13.4	20.4	13.9	37.9	34.2	51.4	-
	NPP [28]	-	-	-	-	-	51.5	66.0	21.22
	OGC [61]	55.6	50.6	65.1	65.0	65.2	60.9	73.4	-
	Ours	63.8	61.3	77.3	84.2	71.3	63.7	75.4	5.47

Experiments

Table 3: *Rigid segmentation results on OGC-DR and OGC-DRSV.*

		AP \uparrow	PQ \uparrow	F1 \uparrow	Pre \uparrow	Rec \uparrow	mIoU \uparrow	RI \uparrow
Supervised Methods	OGC-sup [61]	90.7 / 86.3	82.6 / 78.8	87.6 / 85.0	83.7 / 82.2	92.0 / 88.0	89.2 / 83.9	97.7 / 97.1
	Ours-sup	92.8 / 89.3	86.9 / 82.6	91.0 / 87.9	88.8 / 85.5	93.2 / 90.4	91.2 / 86.6	98.7 / 97.9
Unsupervised Methods	TrajAffn [52]	42.6 / 39.3	46.7 / 43.8	57.8 / 54.8	69.6 / 63.0	49.4 / 48.4	46.8 / 45.9	80.1 / 77.7
	SSC [51]	74.5 / 70.3	79.2 / 75.4	84.2 / 81.5	92.5 / 89.6	77.3 / 74.7	74.6 / 70.8	91.5 / 91.3
	WardLinkage [66]	72.3 / 69.8	74.0 / 71.6	82.5 / 80.5	93.9 / 91.8	73.6 / 71.7	69.9 / 67.2	94.3 / 93.3
	DBSCAN [19]	73.9 / 71.9	76.0 / 76.3	81.6 / 81.8	85.8 / 79.1	77.8 / 84.8	74.7 / 80.1	91.5 / 93.5
	OGC [61]	92.3 / 86.8	85.1 / 77.0	89.4 / 83.9	85.6 / 77.7	93.6 / 91.2	90.8 / 84.8	97.8 / 95.4
	Ours	93.9 / 88.1	87.0 / 80.0	91.1 / 86.1	87.0 / 80.8	95.6 / 92.2	92.4 / 86.7	98.1 / 96.6

Experiments

Table 4: *Rigid segmentation results on KITTI-SF*. Our model still achieves competitive results even though the data setting is inconsistent with the model’s assumption.

Method Category	Method	AP \uparrow	PQ \uparrow	F1 \uparrow	Pre \uparrow	Rec \uparrow	mIoU \uparrow	RI \uparrow
Supervised Methods	OGC-sup [61]	62.4	52.7	65.1	63.4	67.0	67.3	95.0
	Ours-sup	65.1	56.3	68.6	69.4	67.8	69.5	95.7
Unsupervised Methods	TrajAffn [52]	24.0	30.2	43.2	37.6	50.8	48.1	58.5
	SSC [51]	12.5	20.4	28.4	22.8	37.6	41.5	48.9
	WardLinkage [66]	25.0	16.3	22.9	13.7	69.8	60.5	44.9
	DBSCAN [19]	13.4	22.8	32.6	26.7	42.0	42.6	55.3
	OGC [61]	54.4	42.4	52.4	47.3	58.8	63.7	93.6
	Ours	53.6	44.4	55.1	56.3	54.0	61.5	93.4

Experiments

Table 1: Segmentation performance on KITTI-Det.

Methods	AP \uparrow	PQ \uparrow	F1 \uparrow	Pre \uparrow	Rec \uparrow	mIoU \uparrow	RI \uparrow
OGC-sup [10]	51.4	41.0	49.1	43.7	56.0	66.2	91.0
Ours-sup	52.5	43.3	51.8	47.5	57.0	68.0	92.6
OGC-unsup [10]	40.5	30.9	37.0	30.8	46.5	60.6	86.4
Ours-unsup	41.3	32.9	38.8	35.3	43.1	60.2	87.2

Table 2: Segmentation performance on SemanticKITTI.

Sequences	Methods	AP \uparrow	PQ \uparrow	F1 \uparrow	Pre \uparrow	Rec \uparrow	mIoU \uparrow	RI \uparrow
00 - 10	OGC-sup [10]	53.8	41.3	48.1	40.1	60.0	68.3	90.0
	Ours-sup	60.1	47.6	55.4	48.6	64.4	71.9	93.4
	OGC-unsup [10]	42.6	30.2	35.3	28.2	47.3	60.3	86.0
	Ours-unsup	46.9	31.6	36.9	29.0	50.6	63.2	88.7
00 - 07 & 09 - 10	OGC-sup [10]	55.3	41.8	48.4	40.1	61.1	69.9	90.3
	Ours-sup	60.5	48.1	55.6	48.8	64.7	73.2	93.8
	OGC-unsup [10]	43.6	30.5	35.5	28.1	48.2	62.1	86.3
	Ours-unsup	47.4	31.7	36.8	28.7	51.0	64.8	89.3
08	OGC-sup [10]	49.4	39.2	46.6	40.0	55.8	60.3	88.3
	Ours-sup	58.4	46.0	54.4	47.8	63.1	65.8	91.7
	OGC-unsup [10]	38.6	29.1	34.7	28.6	44.0	51.8	84.3
	Ours-unsup	44.2	31.0	37.3	30.0	49.1	55.8	86.1

Q & A