



# FedSR: A Simple and Effective Domain Generalization Method for Federated Learning



A. Tuan Nguyen



Philip Torr



Ser-Nam Lim





# Introduction

---

- ❑ **Federated Learning (FL)** refers to the decentralized and privacy-preserving machine learning framework.
- ❑ There is often **distribution shift** among the clients' data.
- ❑ However, FL techniques often only focus on performance on the source domains/clients, **not** how the model **generalize to an unseen domain** under some distribution shifts.
- ❑ For example, if  $K$  clinical institutions in the US and UK collaborate to train a model with their decentralized data, the goal for the model is not only to perform well on their data distribution, but also to generalize to unseen target data (e.g., from a different country).



# Introduction

---

- ❑ In this paper, we incorporate the **Domain Generalization** (DG) problem into the FL setting to tackle this generalization issue.
- ❑ A common and successful method for DG is **representation alignment**. However, existing works require sharing and comparing data among domains, which is **not allowed in FL**.
- ❑ We propose approaches for **implicit alignment**, that completely respect the the privacy aspect of FL.
- ❑ In particular, we propose to learn a **simple representation** of the data, with a L2-norm regularizer and a conditional mutual information regularizer.
- ❑ We also show that these regularizers help to implicitly aligns the representation.



# Problem Setting

---

- ❑ Representation learning framework:
  - ❑ Representation mapping:  $p(z|x)$
  - ❑ Classifier:  $\hat{p}(y|z)$
- ❑ Predictive distribution:  $\mathbb{E}_{p(z|x)}[\hat{p}(y|x)]$
- ❑ Loss per datapoint  $(x, y)$ :  $-\log \mathbb{E}_{p(z|x)}[\hat{p}(y|x)]$
- ❑ Local loss function of a client/domain  $i$  with data distribution  $p_i(x, y)$   
 $\mathbb{E}_{p_i(x,y)}[-\log \mathbb{E}_{p(z|x)}[\hat{p}(y|x)]]$
- ❑ Global loss over all client:

$$\frac{1}{n\_clients} \sum_i \mathbb{E}_{p_i(x,y)}[-\log \mathbb{E}_{p(z|x)}[\hat{p}(y|x)]]$$



# Approach

---

- ❑ The conventional loss function of FL (previous slide) only focus on performance on the source clients  $i$ 's.
- ❑ To learn a generalizable representation, we propose to use common regularization techniques to restrict the complexity of the representation, hoping that it would learn essential information and ignore spurious correlation.
- ❑ We also show both **theoretically** and **empirically** that these regularizers leads to better marginal and conditional representation alignment.



# Approach: L2-norm Regularizer

---

- We regularize the l2-norm of the representation:

$$\ell_i^{L2R} = \mathbb{E}_{p_i(x)} \left[ \mathbb{E}_{p(z|x)} \left[ \|z\|_2^2 \right] \right]$$

- Connection to **marginal alignment** of the representation (details in our paper).



# Approach: Conditional Mutual Information

---

- We minimize a tractable upper bound of the conditional mutual information  $I_i(x, z|y)$ :

$$\ell_i^{CMI} = \mathbb{E}_{p_i(x,y)} [KL[p(z|x)|r(z|y)]]$$

With  $r(z|y)$  being a learnable variational distribution.

- Connection to **conditional alignment** of the representation (details in our paper).



# Results

Quantitative:

Table 2: PACS. Reported numbers are from 3 runs

Models		Backbone	PACS				Average
			A	C	P	S	
Centralized Methods	DGER [47]	Resnet18	80.70	76.40	96.65	71.77	81.38
	DIRT-GAN [31]	Resnet18	82.56	76.37	95.65	79.89	<b>83.62</b>
FL Methods	FedAVG [28]	Resnet18	77.8±0.5	72.8±0.4	91.9±0.5	78.8±0.3	80.3
	FedADG [45]	Resnet18	77.8±0.5	74.7±0.4	92.9±0.3	79.5±0.4	81.2
	FedCMI (ours)	Resnet18	80.8±0.4	73.7±0.2	92.8±0.5	79.5±0.2	81.7
	FedL2R (ours)	Resnet18	82.2±0.4	75.8±0.3	92.8±0.4	81.6±0.1	83.1
	FedSR (ours)	Resnet18	83.2±0.3	76.0±0.3	93.8±0.5	81.9±0.2	<b>83.7</b>





# Results

Quantitative:

Table 3: **OfficeHome**. Reported numbers are from 3 runs

Models		Backbone	OfficeHome				Average
			A	C	P	R	
Centralized Methods	Mixup [44]	Resnet50	64.7	54.7	77.3	79.2	<b>69.0</b>
	CORAL [38]	Resnet50	64.4	55.3	76.7	77.9	68.6
FL Methods	FedAVG [28]	Resnet50	62.2±0.9	55.6±0.9	75.7±0.2	78.2±0.2	67.9
	FedADG [45]	Resnet50	63.2±0.9	57.0±0.2	76.0±0.1	77.7±0.5	68.4
	FedCMI (ours)	Resnet50	61.8±0.5	55.5±0.9	76.3±0.1	77.4±0.1	67.8
	FedL2R (ours)	Resnet50	64.5±0.3	56.5±0.5	76.1±0.2	77.9±0.2	68.8
	FedSR (ours)	Resnet50	65.4±0.5	57.4±0.2	76.2±0.6	78.3±0.3	<b>69.3</b>



# Results

## Quantitative:

Table 4: **DomainNet**. Reported numbers are from 3 runs

Models		Backbone	DomainNet						
			C	I	P	Q	R	S	AVG
Centralized Methods	MLDG [21]	Resnet50	59.5	19.8	48.3	13.0	59.5	50.4	<b>41.8</b>
	CORAL [38]	Resnet50	58.7	20.9	47.3	13.6	60.2	50.2	<b>41.8</b>
FL Methods	FedAVG [28]	Resnet50	59.3±0.7	16.5±0.9	44.2±0.7	10.8±1.8	57.2±0.8	49.8±0.4	39.6
	FedADG [45]	Resnet50	60.9±0.6	17.2±0.2	44.3±0.2	12.4±0.2	57.6±0.9	50.3±0.8	40.4
	FedCMI (ours)	Resnet50	59.0±0.9	18.0±0.7	44.6±0.5	12.2±0.4	56.2±0.2	50.0±0.4	40.0
	FedL2R (ours)	Resnet50	60.2±0.6	18.1±0.4	44.9±0.6	11.0±0.9	57.8±0.4	51.5±0.7	40.6
	FedSR (ours)	Resnet50	61.0±0.6	18.6±0.4	45.2±0.5	13.4±0.6	57.6±0.2	51.8±0.3	<b>41.3</b>



# Results

**Qualitative:** Our method leads to better alignment of the representation.

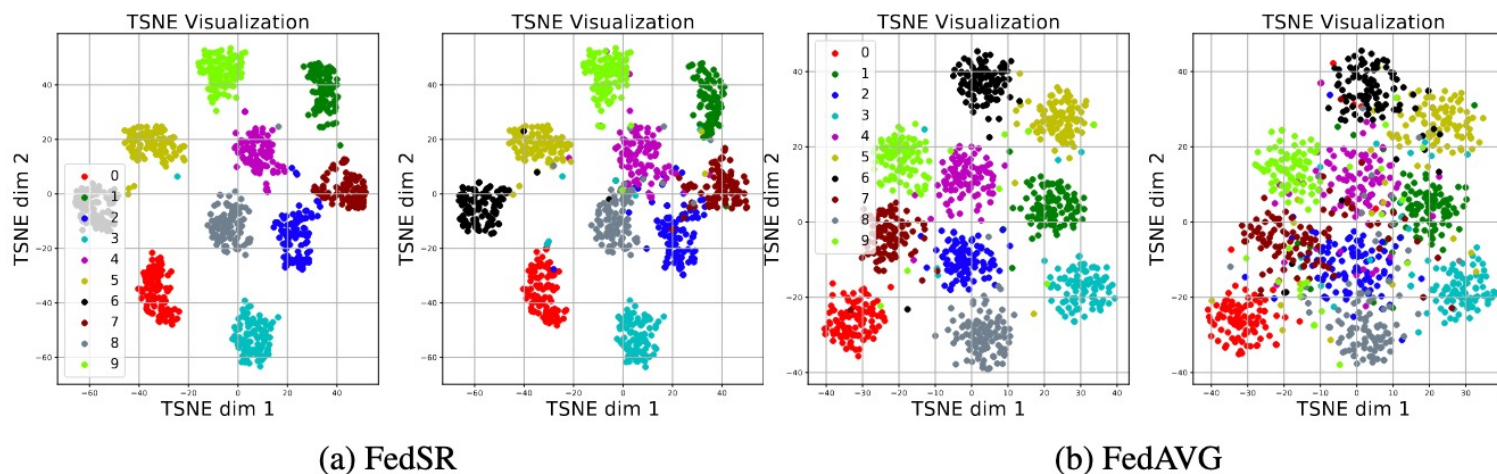


Figure 1: Visualization using t-SNE of the representation space of our method FedSR and the baselines FedAVG. For each method, the left subfigure corresponds to one source domain  $\mathcal{M}_{15}$  and the right one corresponds to the target domain  $\mathcal{M}_0$ . Each color represents a digit class.